

3472/1

Form Four

Additional Mathematics

Paper 1

2009

2 hours

NO.KAD PENGENALAN/I.C NUMBER

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Nama Calon :.....

Tingkatan :

**PEPERIKSAAN SELARAS AKHIR TAHUN
SEKOLAH-SEKOLAH MENENGAH NEGERI MELAKA**

Kelolaan

**PEJABAT PELAJARAN DAERAH
JASIN * ALOR GAJAH * MELAKA TENGAH**

Dengan kerjasama :

**JABATAN PELAJARAN NEGERI MELAKA
TINGKATAN 4 2009**

ADDITIONAL MATHEMATICS
Paper 1
2 hours

**JANGAN BUKA KERTAS SOALANINI
SEHINGGA DIBERITAHU**

1. *Tuliskan nombor kad pengenalan, nama dan tingkatan anda pada ruang yang disediakan.*

Write your I.C. number, name and class in the space provided.

2. *Calon dikehendaki membaca arahan di halaman 2 dan halaman 3*

Candidates are required to read the instructions on page 2 and 3 .

<i>Examiner's Code</i>		
Question	Full Marks	Marks Acquired
1	2	
2	3	
3	3	
4	4	
5	3	
6	3	
7	3	
8	3	
9	3	
10	3	
11	3	
12	3	
13	4	
14	4	
15	3	
16	4	
17	3	
18	3	
19	3	
20	4	
21	3	
22	3	
23	4	
24	3	
25	3	
Total	80	

MAKLUMAT UNTUK CALON

1. *Kertas soalan ini mengandungi 25 soalan.*
2. *Jawab **semua** soalan.*
3. *Bagi setiap soalan berikan **SATU** jawapan sahaja.*
4. *Jawapan hendaklah ditulis dengan jelas dalam ruang yang disediakan dalam kertas soalan.*
5. *Tunjukkan langkah-langkah penting dalam kerja mengira anda. Ini boleh membantu anda untuk mendapatkan markah.*
6. *Sekiranya anda hendak menukar jawapan, batalkan kerja mengira yang telah dibuat. Kemudian tuliskan jawapan yang baru.*
7. *Rajah yang mengiringi soalan tidak dilukiskan mengikut skala kecuali dinyatakan.*
8. *Markah yang diperuntukkan bagi setiap soalan dan ceraian soalan ditunjukkan dalam kurungan.*
9. *Satu senarai rumus disediakan di halaman 4 hingga 6.*
10. *Anda dibenarkan menggunakan kalkulator saintifik yang tidak boleh diprogram.*
11. *Kertas soalan ini hendaklah diserahkan di akhir peperiksaan.*

INFORMATIONS FOR CANDIDATES

1. *This question paper consists of 25 questions.*
2. *Answer **ALL** questions.*
3. *Give only **ONE** answer for each question.*
4. *Write your answer clearly in the spaces provided in the question paper.*
5. *Show your working. It may help you to get marks.*
6. *If you wish to change your answer, cross out the work that you have done. Then write down the new answer.*
7. *The diagram in the questions provided are not drawn to scale unless stated.*
8. *The marks allocated for each question and sub-part of a question are shown in brackets.*
9. *A list of formulae is provided on pages 4 to 6.*
10. *You may use a non-programmable scientific calculator.*
11. *This question paper must be handed in at the end of the examination.*

ALGEBRA

$$1 \quad x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$2 \quad a^m \times a^n = a^{m+n}$$

$$3 \quad a^m \div a^n = a^{m-n}$$

$$4 \quad (a^m)^n = a^{mn}$$

$$5 \quad \log_a mn = \log_a m + \log_a n$$

$$6 \quad \log_a \frac{m}{n} = \log_a m - \log_a n$$

$$7 \quad \log_a m^n = n \log_a m$$

$$8 \quad \log_a b = \frac{\log_c b}{\log_c a}$$

$$9 \quad T_n = a + (n-1)d$$

$$10 \quad S_n = \frac{n}{2} [2a + (n-1)d]$$

$$11 \quad T_n = ar^{n-1}$$

$$12 \quad S_n = \frac{a(r^n - 1)}{r-1} = \frac{a(1-r^n)}{1-r}, r \neq 1$$

$$13 \quad S_\infty = \frac{a}{1-r}, |r| < 1$$

CALCULUS

$$1 \quad y = uv, \quad \frac{dy}{dx} = u \frac{dv}{dx} + v \frac{du}{dx}$$

$$2 \quad y = \frac{u}{v}, \quad \frac{dy}{dx} = \frac{v \frac{du}{dx} - u \frac{dv}{dx}}{v^2}$$

$$3 \quad \frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx}$$

$$4 \quad \text{Area under a curve} = \int_a^b y \, dx \quad \text{or}$$

$$\int_a^b x \, dy$$

$$5 \quad \begin{aligned} &\text{Volume generated} \\ &= \int_a^b \pi y^2 \, dx \quad \text{or} \end{aligned}$$

$$= \int_a^b \pi x^2 \, dy$$

STATISTICS

$$1 \quad \bar{x} = \frac{\Sigma x}{N}$$

$$2 \quad \bar{x} = \frac{\Sigma fx}{\Sigma f}$$

$$3 \quad \sigma = \sqrt{\frac{\Sigma(x - \bar{x})^2}{N}} = \sqrt{\frac{\Sigma x^2}{N} - \bar{x}^2}$$

$$4 \quad \sigma = \sqrt{\frac{\Sigma f(x - \bar{x})^2}{\Sigma f}} = \sqrt{\frac{\Sigma fx^2}{\Sigma f} - \bar{x}^2}$$

$$8 \quad {}^n P_r = \frac{n!}{(n-r)!}$$

$$9 \quad {}^n C_r = \frac{n!}{(n-r)!r!}$$

$$10 \quad P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$11 \quad P(X = r) = {}^n C_r p^r q^{n-r}, p + q = 1$$

$$5 \quad m = L + \left(\frac{\frac{1}{2}N - F}{f_m} \right) C$$

$$12 \quad \text{Mean} = np$$

$$6 \quad I = \frac{Q_1}{Q_0} \times 100$$

$$13 \quad \sigma = \sqrt{npq}$$

$$7 \quad \bar{I} = \frac{\sum W_i I_i}{\sum W_i}$$

$$14 \quad Z = \frac{X - \mu}{\sigma}$$

GEOMETRY

$$1 \quad \text{Distance} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$4 \quad \text{Area of a triangle} =$$

$$\frac{1}{2} |(x_1 y_2 + x_2 y_3 + x_3 y_1) - (x_2 y_1 + x_3 y_2 + x_1 y_3)|$$

$$2 \quad \text{Midpoint} = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

$$5. \quad \left| \begin{smallmatrix} r \\ \sim \end{smallmatrix} \right| = \sqrt{x^2 + y^2}$$

$$3 \quad \text{A point dividing a segment of a line} \\ (x, y) = \left(\frac{nx_1 + mx_2}{m+n}, \frac{ny_1 + my_2}{m+n} \right)$$

$$6 \quad \hat{r} = \frac{x \hat{i} + y \hat{j}}{\sqrt{x^2 + y^2}}$$

TRIGONOMETRY

$$1 \quad \text{Arc length, } s = r\theta$$

$$8 \quad \sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$$

$$2 \quad \text{Area of a sector, } A = \frac{1}{2} r^2 \theta$$

$$9 \quad \cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$$

$$3. \quad \sin^2 A + \cos^2 A = 1$$

$$10 \quad \tan(A \pm B) = \frac{\tan A \pm \tan B}{1 \mp \tan A \tan B}$$

$$4 \quad \sec^2 A = 1 + \tan^2 A$$

$$11 \quad \tan 2A = \frac{2 \tan A}{1 - \tan^2 A}$$

$$5 \quad \csc^2 A = 1 + \cot^2 A$$

$$12 \quad \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$6 \quad \sin 2A = 2 \sin A \cos A$$

$$13 \quad a^2 = b^2 + c^2 - 2bc \cos A$$

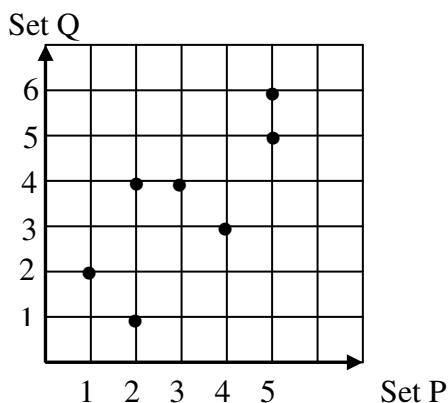
$$7 \quad \cos 2A = \cos^2 A - \sin^2 A$$

$$= 2 \cos^2 A - 1$$

$$= 1 - 2 \sin^2 A$$

$$14 \quad \text{Area of triangle} = \frac{1}{2} ab \sin C$$

*Answer all questions.
Jawab semua soalan.*

1.

The graph above shows the relation between set P and set Q.

Graf di atas menunjukkan hubungan di antara set P dan set Q.

- (a) State the object of image 5.

Nyatakan objek bagi imej 5.

- (b) State the type of relation.

[2 marks]

Nyatakan jenis hubungan.

Answer : (a)

(b)

1**2**

-
2. Given that $f(x) = |3x - 8|$, find the value of

Diberi bahawa $f(x) = |3x - 8|$, cari nilai

- (a) $f(-2)$

- (b) the objects which mapped onto 4.

[3 marks]

objek yang dipetakan kepada 4.

Answer : (a)

(b)

2**3**

3. Given the function $f: x \rightarrow x + 1$ and $g: x \rightarrow 2x + 1$, find

Diberi fungsi $f: x \rightarrow x + 1$ dan $g: x \rightarrow 2x + 1$, cari

(a) $gf(x)$

(b) the value of x if $gf(x) = 7x - 2$

nilai x jika $gf(x) = 7x - 2$

[3 marks]

3

3
3

Answer : (a).....

(b).....

-
4. Given the function $f: x \rightarrow \frac{2x}{x-a}$, $x \neq a$. Find

Diberi fungsi $f: x \rightarrow \frac{2x}{x-a}$, $x \neq a$. Cari

(a) the value of a if $f(8) = 4$,

nilai a jika $f(8) = 4$,

(b) $f^{-1}(3)$

[4 marks]

4

4
4

Answer : (a).....

(b)

5. The roots of the equation $ax^2 + bx - 6 = 0$ are -2 and $\frac{3}{4}$. Find the values of a and b .

Punca-punca persamaan $ax^2 + bx - 6 = 0$ ialah -2 and $\frac{3}{4}$. Cari nilai-nilai a dan b .

[3 marks]

Answer : $a = \dots\dots\dots\dots$

$b = \dots\dots\dots\dots$

5

3

6. The quadratic equation $x^2 - 2x + 1 = k(-x - 2)$ has two real and equal roots. Find the possible values of k .

Persamaan kuadratik $x^2 - 2x + 1 = k(-x - 2)$ mempunyai dua nilai nyata yang sama. Cari nilai-nilai k yang mungkin.

[3 marks]

6

3

Answer : $\dots\dots\dots\dots$

7. Given that α and β are the roots of the quadratic equation $x^2 - 6x + 5 = 0$, form the

quadratic equation whose roots are $\frac{1}{\alpha}$ and $\frac{1}{\beta}$.

[3 marks]

Diberi bahawa α dan β adalah nilai-nilai punca bagi persamaan quadratik $x^2 - 6x + 5 = 0$, bentukkan persamaan kuadratik yang mempunyai punca-punca $\frac{1}{\alpha}$ and $\frac{1}{\beta}$.

7

3

Answer : $\dots\dots\dots\dots$

[See overleaf]
SULIT

8. Solve the quadratic equation $5x(1 - 2x) = (x - 1)(x + 4)$. Give your answers correct to four significant figures. [3 marks]
Selesaikan persamaan kuadratik $5x(1 - 2x) = (x - 1)(x + 4)$. Beri jawapan anda kepada empat angka bererti.

8

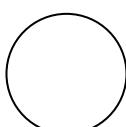
3

Answer :

-
9. By the method of completing the square, find the coordinates of the minimum point of $y = x^2 - 6x + 7$. [3 marks]
Dengan menggunakan kaedah penyempurnaan kuasa dua, tentukan koordinat titik minimum bagi $y = x^2 - 6x + 7$.

9

3

Answer :

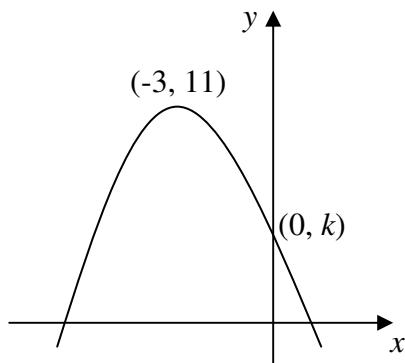
10.

Diagram 1
Rajah 1

Diagram 1 shows part of the graph of the function $y = p - (x + n)^2$, where p and n are constants. Find the value of

Rajah 1 menunjukkan sebahagian daripada graf fungsi $y = p - (x + n)^2$, di mana p dan n adalah pemalar.
Cari nilai

- (a) p ,
- (b) n
- (c) k

[3 marks]

Answer : $p = \dots \dots \dots$

$n = \dots \dots \dots$

$k = \dots \dots \dots$

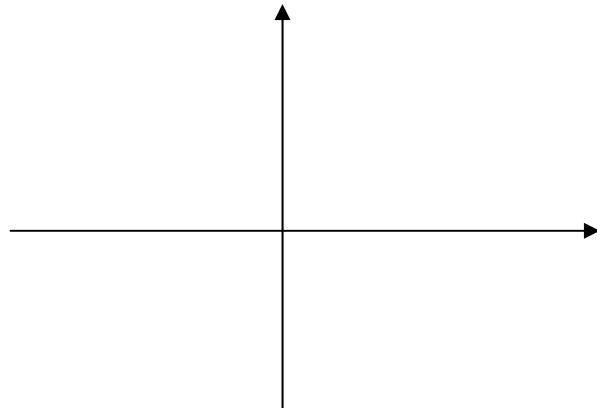
10

3

11. Given the function $y = 3 - (x + 2)^2$. Sketch the curve of the function. [3 marks]

Diberi fungsi $y = 3 - (x + 2)^2$. Lakarkan garis lengkung fungsi itu.

Answer :



11

3

[See overleaf]
SULIT

12. Solve $4^{3x} - 16^{x+1} = 0$.

[3 marks]

Selesaikan $4^{3x} - 16^{x+1} = 0$.

12

3

Answer :

13. Solve $2\log_5 2 + \log_5(4x-1) = 1 + \log_5(x+8)$.

[4 marks]

Selesaikan $2\log_5 2 + \log_5(4x-1) = 1 + \log_5(x+8)$.

13

4

Answer :

14. Solve $\log_2 x - \log_4 x = -2$.

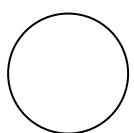
[4 marks]

Selesaikan $\log_2 x - \log_4 x = -2$.

14

4

Answer :



- 15.** Express $3^{n+2} - 3^n + 10(3^{n-1})$ in the simplest form.

[3 marks]

Ungkapkan $3^{n+2} - 3^n + 10(3^{n-1})$ dalam bentuk yang termudah.

15

3

Answer :

- 16.**

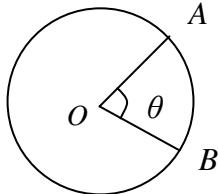


Diagram 2
Rajah 2

Diagram 2 shows a circle with centre O . The length of the minor arc AB is 12.4 and the angle of the major sector AOB is 330° . Using $\pi = 3.142$, find

Rajah 2 menunjukkan sebuah bulatan yang berpusat O . Panjang lengkuk minor AB ialah 12.4 dan sudut sektor major AOB ialah 330° . Dengan menggunakan $\pi = 3.142$, cari

- the value of θ in radians. (Give your answer correct to four significant figures)
nilai θ dalam radian. (Beri jawapan anda betul kepada empat angka bererti)
- the length, in cm, of the radius of the circle.
panjang jejari bulatan dalam cm.

[4 marks]

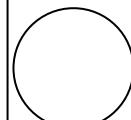
Answer : (a)

(b).....

16

4

[See overleaf]
SULIT



17. Diagram 3 shows a sector OLM with centre O .

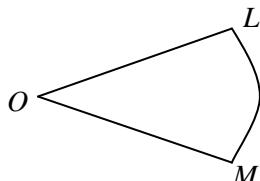


Diagram 3
Rajah 3

Given $OL = 12 \text{ cm}$ and the length of arc $LM = 14.4 \text{ cm}$. Find $\angle LOM$, in degree and minutes. (use $\pi = 3.142$) [3 marks]

Diberi $OL = 12 \text{ cm}$ dan panjang lengkuk $LM = 14.4 \text{ cm}$. Cari $\angle LOM$, dalam darjah dan minit. (gunakan $\pi = 3.142$)

17

3

Answer :

18. The perimeter of a sector of a circle with radius 4 cm is 20 cm. Find the area of the sector. [3 marks]

Perimeter sektor suatu bulatan dengan jejari 4 cm ialah 20 cm. Cari luas sektor tersebut.

18

3

Answer :

19. Differentiate $3x^5(2x - 7)^4$ with respect to x . [3 marks]

Bezakan $3x^5(2x - 7)^4$ terhadap x .

19

3

Answer :

- 20.** Given that $y = 3x^2 - x + 4$,

Diberi bahawa $y = 3x^2 - x + 4$,

- (a) find the value of $\frac{dy}{dx}$ when $x = 2$,

cari nilai $\frac{dy}{dx}$ apabila $x = 2$,

- (b) calculate the small change in y when x increases from 2 to 2.5. [4 marks]

kirakan perubahan kecil y apabila x bertambah dari 2 kepada 2.5

20

Answer : (a).....

4

(b).....

-
- 21.** A set of data consists of five numbers. The sum of the numbers is 175 and the sum of the squares of the numbers is 6845. Find,

Satu set data mengandungi lima nombor. Hasil tambah nombor-nombor itu ialah 175 dan hasil tambah kuasa dua nombor-nombor ialah 6845. Cari,

- (a) the mean,

min

- (b) the standard deviation.

sisisian piawai.

for the five numbers

bagi lima nombor itu

[3 marks]

21

Answer : (a)

3

(b)

[See overleaf]

SULIT

22. The curve $y = -2x^2 + 8x - 3$ has a maximum point at $x = p$, where p is a constant.
Find the value of p . [3 marks]
Suatu lengkung $y = -2x^2 + 8x - 3$ mempunyai titik maksimum di $x = p$, di mana p ialah pemalar.
Cari nilai p .

22

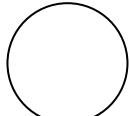
3

Answer : $p = \dots \dots \dots$

-
23. The radius of a spherical balloon is increasing at the rate of $x \text{ cms}^{-1}$.
Given that the rate of change of the volume of the balloon is $25\pi \text{ cm}^3 \text{ s}^{-1}$ when
its radius is 5 cm. Find the value of x . [$V = \frac{4}{3}\pi r^3$] [4 marks]
*Jejari untuk suatu belon sfера bertambah dengan kadar $x \text{ cms}^{-1}$. Diberi kadar perubahan isipadu bagi
belon ialah $25\pi \text{ cm}^3 \text{ s}^{-1}$ apabila jejari nya ialah 5 cm.*
Cari nilai x . [$V = \frac{4}{3}\pi r^3$]

23

4

Answer : $x = \dots \dots \dots$

24. A set of 8 numbers has a mean of 16.8 and a standard deviation of 2.5.

If every number of the set of data is multiplied by 2 and then added by 3, find

Satu set lapan nombor mempunyai min 16.8 dan sisihan piawai 2.5. Jika setiap nombor dalam set data didarabkan dengan 2 dan kemudianya ditambah dengan 3, cari

- (a) the new mean,
min baru
(b) the new standard deviation of the set of data. [3 marks]
sisihan piawai baru bagi set data itu.

24

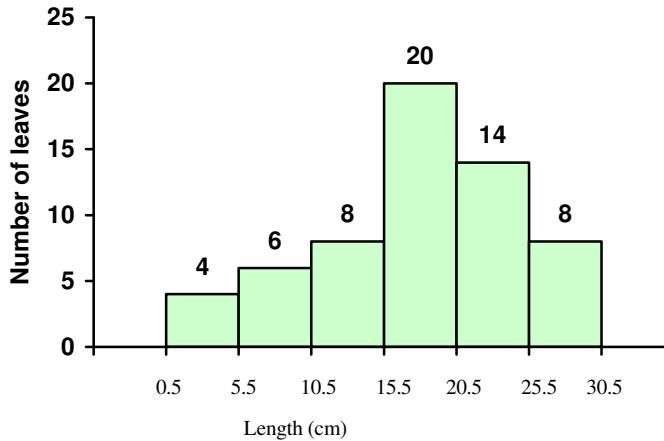
Answer : (a)

(b).....

3

25. The diagram below shows a histogram which represent the distribution of the length of 60 leaves collected from a garden.

Rajah di bawah menunjukkan satu histogram yang mewakili taburan panjang bagi 60 keping daun yang dikumpul dari taman.



Without using an ogive, calculate the median.

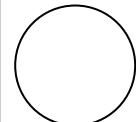
Tanpa menggunakan ogif, hitungkan median panjang.

[3 marks]

25

Answer :

3



END OF QUESTION PAPER

[See overleaf]

**SULIT
3472/1
Additional
Mathematics
Paper 1
2009**

**PEJABAT PENDIDIKAN DAERAH
JASIN * ALOR GAJAH * MELAKA TENGAH
JABATAN PENDIDIKAN MELAKA
KEMENTERIAN PELAJARAN MALAYSIA**

**PEPERIKSAAN AKHIR TAHUN
TINGKATAN 4**

2009

ADDITIONAL MATHEMATICS

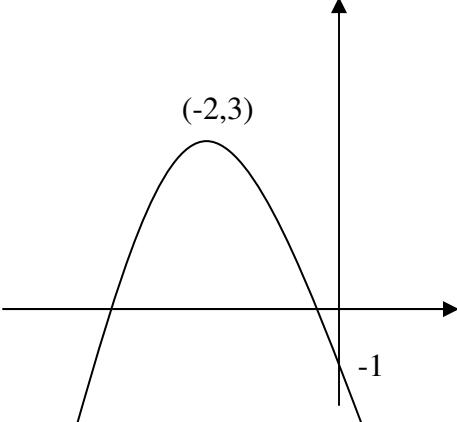
Paper 1

MARKING SCHEME

This marking scheme consists of 6 printed pages

PAPER 1 MARKING SCHEME FORM 4 2009 (PEP. AKHIR TAHUN)
3472/1

Number	Solution and marking scheme	Sub Marks	Full Marks
1 (a) (b)	5 Many-to-many	1 1	2
2 (a) (b)	14 $x = 4$ or $x = \frac{4}{3}$ B1 : $4 = 3x - 8$	1 2	3
3 (a) (b)	$2x + 3$ B1 : $2(x + 1) + 1$ $x = 1$	2 1	3
4 (a) (b)	$a = 4$ B1 : $\frac{2(8)}{8-a} = 4$ $x = 12$ $f^{-1}(3) = x$ $f(x) = 3$ B1: $\frac{2x}{x-4} = 3$	2 2	4
5	$a = 4, b = 5$ B1 : $x^2 - (-2 + \frac{3}{4})x + (-2)(\frac{3}{4}) = 0$ or $(x + 2)(4x - 3) = 0$	3 2	3
6	$k = 0$ or 12 B2 : $k^2 - 12k = 0$ B1: $(-2 + k)^2 - 4(1)(1 + 2k) = 0$	3 2 1	3

Number	Solution and marking scheme	Sub Marks	Full Marks
7	$5x^2 - 6x + 5 = 0$ or equivalent B2: $\frac{1}{\alpha} + \frac{1}{\beta} = \frac{6}{7}$, $(\frac{1}{\alpha})(\frac{1}{\beta}) = \frac{4}{7}$ B1: $\alpha + \beta = 6$ or $\alpha\beta = 5$	3 2 1	3
8	0.7007 and -0.5189 B2: $\frac{-(-2) \pm \sqrt{(-2)^2 - 4(11)(-4)}}{2(11)}$ B1: $11x^2 - 2x - 4 = 0$	3 2 1	3
9	Minimum point (3, -2) B2: $(x-3)^2 - 2$ B1: $x^2 - 6x + \left(-\frac{6}{2}\right)^2 - \left(-\frac{6}{2}\right)^2 + 7$	3 2 1	3
10	$p = 11$, $n = 3$, $k = 2$	1 1 1	3
11	 B2: Shape and maximum point or y-intercept B1: Shape	3 2 1	3
12	$x = 2$ B2: $3x = 2x + 2$ B1: $4^{3x} = 4^{2x+2}$	3 2 1	3

Number	Solution and marking scheme	Sub Marks	Full Marks
13	$x = 4$ B3: $16x - 4 = 5x + 40$ B2 : $\log_5(2^2(4x-1)) = \log_5 5(x+8)$ B1 : $\log_5 2^2$ or $\log_5 5$	4 3 2 1	4
14	$x = \frac{1}{16}$ B3 : $x(x^{-\frac{1}{2}}) = \frac{1}{4}$ B2 : $\log_2 \frac{x}{\sqrt{x}} = \log_2 \frac{1}{4}$ B1: $\frac{\log_2 x}{\log_2 4}$ or $\log_2 2^{-2}$	4 3 2 1	4
15	$3^n \left(\frac{34}{3}\right)$ or $34 \left(3^{n-1}\right)$ B2 : $3^n \left(3^2 - 1 + \frac{10}{3}\right)$ B1 : $3^n \left(3^2\right) - 3^n + 10 \left(\frac{3^n}{3^1}\right)$	3 2 1	3
16	a) 0.5237 B1 : seen 30° b) 23.68 B1: $\frac{12.4}{0.5237}$	2 1 2 1	4

Number	Solution and marking scheme	Sub Marks	Full Marks
17	68.75° or $68^0 45'$ B2: $1.2 \times \frac{180^\circ}{3.142}$ B1: 1.2	3 2 1	3
18	24 B2 : $\frac{1}{2}(4)^2(3)$ B1: 12 @ 3	3 2 1	3
19	$3x^4(18x - 35)(2x - 7)^3$ B2 : $3x^5 \cdot 8(2x - 7)^3 + (2x - 7)^4(15x^4)$ B1 : $15x^4$ @ $8(2x - 7)^3$	3 2 1	3
20	a) 11 B1: $6x - 1$ b) 5.5 B1: Seen : 0.5	2 1 2 1	4
21	(a) mean = 35 (b) 12 B1: $\sqrt{\frac{6845}{5} - (35)^2}$ or equivalent	1 2	3
22	p = 2 B2 : $x - 2 = 0$ or $-4p + 8 = 0$ B1 : $-2 \left[(x-2)^2 - (-2)^2 + \frac{3}{2} \right]$ or $\frac{dy}{dx} = -4x + 8$	3 2 1	3

Number	Solution and marking scheme	Sub Marks	Full Marks
23	<p>0.25</p> <p>B3 : $\frac{dv}{dt} = \frac{25}{(4)(5^2)}$ or equivalent</p> <p>B2: $\frac{dr}{dt} = 4 \pi r^2$</p> <p>B1 : $\frac{dr}{dt} = x \text{ cms}^{-1}$ or $\frac{dv}{dt} = 25 \pi \text{ cms}^{-1}$</p>	4 3 2 1	4
24	<p>(a) $(16.8 \times 2) + 3 = 36.6$</p> <p>(a) $2.5 \times 2 = 5$</p>	2 1	3
25	<p>18.5</p> <p>B2: $M = 15.5 + \left(\frac{\frac{1}{2}(60) - 18}{20} \right) 5$</p> $= 15.5 + 3$ <p>B1: 15.5 or 18 or 20 substitute correctly</p>	3 2 1	3

3472/2
Form 4
Additional Mathematics
Paper 2
2009

$2\frac{1}{2}$ hours



**PEPERIKSAAN SELARAS AKHIR TAHUN
SEKOLAH-SEKOLAH MENENGAH NEGERI MELAKA**
Kelolaan
PEJABAT PELAJARAN DAERAH
JASIN * ALOR GAJAH * MELAKA TENGAH
Dengan kerjasama :
JABATAN PELAJARAN NEGERI MELAKA
TINGKATAN 4 2009

ADDITIONAL MATHEMATICS

Paper 2

$2\frac{1}{2}$ hours

JANGAN BUKA KERTAS SOALANINI SEHINGGA DIBERITAHU

1. *This question paper consists of three sections : Section A, Section B and Section C.*
 2. *Answer all question in Section A , four questions from Section B and two questions from Section C.*
 3. *Give only one answer / solution to each question..*
 4. *Show your working. It may help you to get marks.*
 5. *The diagram in the questions provided are not drawn to scale unless stated.*
 6. *The marks allocated for each question and sub-part of a question are shown in brackets..*
 7. *A list of formulae is provided on pages 2 to 3.*
 8. *A booklet of four-figure mathematical tables is provided.*
 9. *You may use a non-programmable scientific calculator.*
-

Kertas soalan ini mengandungi 11 halaman bercetak

The following formulae may be helpful in answering the questions. The symbols given are the ones commonly used

ALGEBRA

1
$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

2
$$a^m \times a^n = a^{m+n}$$

3
$$a^m \div a^n = a^{m-n}$$

4
$$(a^m)^n = a^{nm}$$

5
$$\log_a mn = \log_a m + \log_a n$$

6
$$\log_a \frac{m}{n} = \log_a m - \log_a n$$

7
$$\log_a m^n = n \log_a m$$

8
$$\log_a b = \frac{\log_c b}{\log_c a}$$

9
$$T_n = a + (n-1)d$$

10
$$S_n = \frac{n}{2}[2a + (n-1)d]$$

11
$$T_n = ar^{n-1}$$

12
$$S_n = \frac{a(r^n - 1)}{r-1} = \frac{a(1 - r^n)}{1-r}, (r \neq 1)$$

13
$$S_\infty = \frac{a}{1-r}, |r| < 1$$

CALCULUS

1
$$y = uv, \frac{dy}{dx} = u \frac{dv}{dx} + v \frac{du}{dx}$$

$$= \int_a^b y \, dx \text{ or}$$

2
$$y = \frac{u}{v}, \frac{dy}{dx} = \frac{v \frac{du}{dx} - u \frac{dv}{dx}}{v^2},$$

$$= \int_a^b x \, dy$$

5 Volume generated

$$= \int_a^b \pi y^2 \, dx \text{ or}$$

$$= \int_a^b \pi x^2 \, dy$$

GEOMETRY

1 Distance $= \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$

5 A point dividing a segment of a line

2 Midpoint $(x, y) = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$

$$(x, y) = \left(\frac{nx_1 + mx_2}{m+n}, \frac{ny_1 + my_2}{m+n} \right)$$

3 $|r| = \sqrt{x^2 + y^2}$

6. Area of triangle =

4
$$\hat{r} = \frac{xi + yj}{\sqrt{x^2 + y^2}}$$

$$\frac{1}{2} |(x_1y_2 + x_2y_3 + x_3y_1) - (x_2y_1 + x_3y_2 + x_1y_3)|$$

[Lihat sebelah
SULIT

STATISTICS

$$1 \quad \bar{x} = \frac{\sum x}{N}$$

$$2 \quad \bar{x} = \frac{\sum fx}{\sum f}$$

$$3 \quad \sigma = \sqrt{\frac{\sum (x - \bar{x})^2}{N}} = \sqrt{\frac{\sum x^2}{N} - \bar{x}^2}$$

$$4 \quad \sigma = \sqrt{\frac{\sum f(x - \bar{x})^2}{\sum f}} = \sqrt{\frac{\sum fx^2}{\sum f} - \bar{x}^2}$$

$$5 \quad M = L + \left[\frac{\frac{1}{2}N - F}{f_m} \right] C$$

$$6 \quad I = \frac{P_1}{P_0} \times 100$$

$$7 \quad \bar{I} = \frac{\sum w_i I_i}{\sum w_i}$$

$$8 \quad {}^n P_r = \frac{n!}{(n-r)!}$$

$$9 \quad {}^n C_r = \frac{n!}{(n-r)!r!}$$

$$10 \quad P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$11 \quad p(X=r) = {}^n C_r p^r q^{n-r}, \quad p+q=1$$

$$12 \quad \text{Mean, } \mu = np$$

$$13 \quad \sigma = \sqrt{npq}$$

$$14 \quad z = \frac{x - \mu}{\sigma}$$

TRIGONOMETRY

$$1 \quad \text{Arc length, } s = r\theta$$

$$9 \quad \sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$$

$$2 \quad \text{Area of sector, } A = \frac{1}{2}r^2\theta$$

$$10 \quad \cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$$

$$3 \quad \sin^2 A + \cos^2 A = 1$$

$$11 \quad \tan(A \pm B) = \frac{\tan A \pm \tan B}{1 \mp \tan A \tan B}$$

$$4 \quad \sec^2 A = 1 + \tan^2 A$$

$$12 \quad \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$5 \quad \operatorname{cosec}^2 A = 1 + \cot^2 A$$

$$13 \quad a^2 = b^2 + c^2 - 2bc \cos A$$

$$7 \quad \cos 2A = \cos^2 A - \sin^2 A \\ = 2 \cos^2 A - 1 \\ = 1 - 2 \sin^2 A$$

$$14 \quad \text{Area of triangle} = \frac{1}{2}ab \sin C$$

$$8 \quad \tan 2A = \frac{2 \tan A}{1 - \tan^2 A}$$

**Section A
(40 marks)***Answer all questions*

1. Solve the following simultaneous equations:

Selesaikan persamaan serentak berikut:

$$x^2 - 6y + y^2 = 2x + 2y = 16 \quad [5 \text{ marks}]$$

2. Given that $f: x \rightarrow 2x - 1$ and $g: x \rightarrow \frac{x}{3} + 1$, find

Diberi $f: x \rightarrow 2x - 1$ dan $g: x \rightarrow \frac{x}{3} + 1$, cari

- (a) $f^{-1}(x)$, [1 mark]
(b) $f^{-1}g(x)$, [2 marks]
(c) $h(x)$ such that $hg(x) = 3x + 6$.
h(x) di mana $hg(x) = 3x + 6$. [3 marks]

3. Solve the following equations.

Selesaikan persamaan berikut.

(a) $2^{x+3} - 2^{x+2} = 2$ [3 marks]

(b) $\log_9(x+9) = 3 \log_9 5$ [3 marks]

- 4.) (a) A set of data consists of four numbers. Given that $\sum x = 12k$ and $\sum x^2 = 100$.

Express the variance in terms of k .

*Diberi satu kumpulan data mengandungi empat nombor. Diberi $\sum x = 12k$ dan $\sum x^2 = 100$.**Ungkapkan varians dalam sebutan k .* [3 marks]

- (b) A set of positive integers $1, m - 1, 6$ and 8 is arranged in ascending order.

Find the value of m if

*Satu set integer positif $1, m - 1, 6$ dan 8 disusun dalam bentuk susunan menaik.**Cari nilai m jika*

(i) the mode is 1 , [3 marks]
mod adalah 1 ,

(ii) the mean is 4 . [3 marks]
min adalah 4 .

5. It is given that the equation of a curve is $y = x^2 - 8x + 4$.

Find

*Diberi satu persamaan lengkung adalah $y = x^2 - 8x + 4$.**Cari*

[Lihat sebelah
SULIT

- (a) the turning point of the curve. [3 marks]
Titik pertukaran lengkung tersebut
- (b) the value of x if $y \frac{d^2y}{dx^2} + x \frac{dy}{dx} + 12 = 0$ [4 marks]
nilai x jika $y \frac{d^2y}{dx^2} + x \frac{dy}{dx} + 12 = 0$
6. (a) If the line $x - y = 4k + 2$ does not meet the curve $y = k(x+1)(x-3)$, find the range of values of k . [5 marks]
Jika garis lurus $x - y = 4k + 2$ tidak bersilang dengan garis lengkung $x - y = 4k + 2$, cari julat nilai k
- (b) $f(x) = x^2 - 6hx + 8h^2 + 1$ has a minimum value of $t + 2h^2$, where t and h are constants. By completing the square, show that $t = 1 - 3h^2$ [3 marks]
 $f(x) = x^2 - 6hx + 8h^2 + 1$ mempunyai nilai minimum $t + 2h^2$, di mana t dan h adalah malar.
Menggunakan penyempurnaan kuasa dua, tunjukkan bahawa $t = 1 - 3h^2$

Section B

(40 Marks)

Answer four questions from this Section.

7. A point P moves so that its distance from point $R(4,3)$ is always 2 units. The point S moves such that it is always equidistant from point $Q(6,5)$ and point R .

Satu titik P bergerak di mana jaraknya dari titik $R(4,3)$ senantiasa 2 unit. Satu titik S pula bergerak senantiasa sama jarak dari titik $Q(6,5)$ dan titik R .

- (a) Find the equation of locus of point S . [3 marks]

Cari persamaan lokus titik S

- (b) Show that the equation of locus of point P is $x^2 + y^2 - 8x - 6y + 21 = 0$. [2 marks]

Tunjukkan bahawa persamaan titik P adalah $x^2 + y^2 - 8x - 6y + 21 = 0$.

- (c) Find the point of intersections of the two loci. [3 marks]

Cari titik persilangan dua lokus tersebut.

- (d) Determine whether the midpoint of QR lies on the locus of point P . [2 marks]

Tentukan sama ada titik tengah QR berada di atas titik P

8.

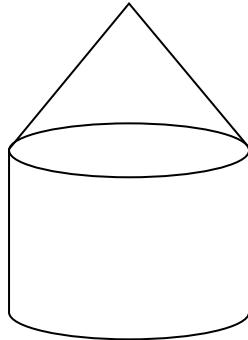


Diagram 1

Diagram 1 shows a composite solid such that a cone is placed on top of a cylinder. Given the radius of a cylinder is x cm, the slant height of cone is $2x$ cm and the volume of a cylinder is 24π cm³.

Rajah 1 menunjukkan gabungan bongkah padu di mana sebuah kon diletakkan ke atas sebuah silinder. Diberi juga jejari silinder tersebut adalah x cm, ketinggian condong kon adalah $2x$ cm dan isi padu silinder adalah 24π cm³.

- (a) Show that the total surface area of the composite solid, A cm², is given by

$$A = 3\pi(x^2 + \frac{16}{x}). \quad [3 \text{ marks}]$$

Tunjukkan bahawa jumlah luas permukaan bongkah padu tersebut, A cm², adalah

$$A = 3\pi(x^2 + \frac{16}{x}).$$

- (b) Calculate the minimum value of total surface area of a solid. [3 marks]

Hitung nilai minimum bagi luas permukaan bongkah tersebut.

- (c) Given the total surface area of the solid increases at the rate of 42π cm²s⁻¹. Find the rate of change of its radius when the radius is 4 cm. [2 marks]

Diberi bahawa luas permukaan menokok pada kadar 42π cm²s⁻¹, cari kadar perubahan jejari pada ketika jejari 4 cm.

- (d) Given the radius of cylinder increases from 4 cm to 4.003 cm. Calculate the small changes in total surface area of the solid. [2 marks]

Diberi jejari silinder menokok dari 4 cm ke 4.003 cm, hitungkan tokokan kecil luas permukaan bongkah.

9. The table 2 below shows the frequency distribution of scores obtained by a group of students.

Jadual 2 dibawah menunjukkan taburan kekerapan markah yang didapati oleh sekumpulan pelajar.

Marks	Number of candidates
1 - 5	3
6 - 10	5
11 - 15	6
16 - 20	k
21 - 25	2
26 - 30	1

TABLE 2

Given the first quartile score of the distribution is 7.5.

Diberi kuartil pertama bagi taburan markah tersebut adalah 7.5

- (a) Find the value of k.

Carikan nilai k

[3 marks]

- (b) Calculate the standard deviation of the distribution.

Hitungkan sisihan piawai bagi taburan itu

[3 marks]

- (c) By drawing histogram, estimate the modal score.

Dengan melukis histogram, anggarkan skor mod

[4 marks]

10.

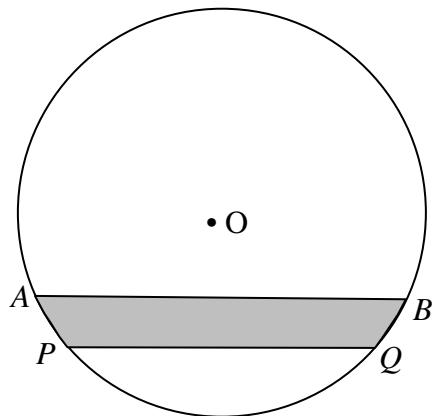


Diagram 2

Diagram 2 shows a circle, centre O, radius 8 cm, with point A, B, P and Q lies on its circumference. Given AB is parallel to PQ, $PQ = 8 \text{ cm}$ and $\angle AOB = 100^\circ$.

Rajah 2 menunjukkan sebuah bulatan berpusat O, berjejari 8 cm dan titik-titik A, B, P dan Q berada di atas lilitan bulatan. Diberi AB adalah selari dengan PQ dan $PQ = 8 \text{ cm}$ dan $\angle AOB = 100^\circ$.

Find

Cari

- (a) $\angle POQ$.

[1 marks]

- (b) length of arc AP

panjang lengkuk AP

[2 marks]

[Lihat sebelah
SULIT

- (c) perimeter of shaded region.

perimeter rantau berlorek

[3 marks]

- (d) area of shaded region

luas rantau berlorek

[4 marks]

11. Diagram 4 shows three vertices of a parallelogram $ABCD$.

Rajah 4 menunjukkan tiga bucu sebuah segiempat selari $ABCD$.

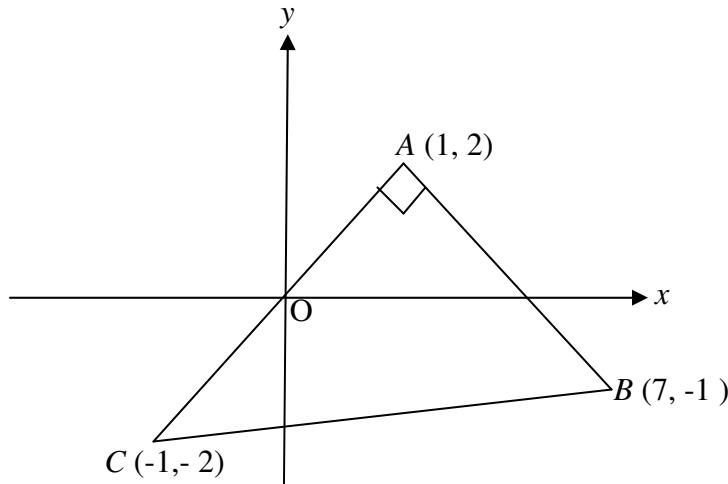


Diagram 4

- (a) Prove that $\angle BAC = 90^\circ$.

Buktikan $\angle BAC = 90^\circ$.

[2 marks]

- (b) Find the coordinate of D and , hence find the area of the parallelogram.

Cari koordinat D dan seterusnya, cari luas segiempat selari ini.

[4 marks]

- (c) The points A , B , C and $Q(x,y)$ lie on the circumference of a circle. Find the coordinate of the circle and the equation of the locus Q

Titik –titik A , B , C dan $Q(x, y)$ terletak pada lilitan sebuah bulatan. Cari koordinat pusat bulatan tersebut dan persamaan lokus bagi titik Q .

[4 marks]

Section C

(20 Marks)

Answer **two** questions from this Section.

12. The diagram 4 shows a triangle PQR .

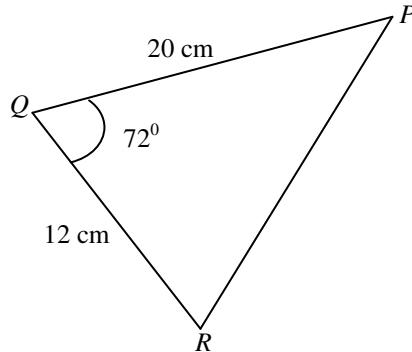
Rajah 4 menunjukkan segi tiga PQR 

Diagram 4

- (a) Calculate the length, in cm, of PR

Hitungkan, dalam cm, panjang PR

[2 marks]

- (b) A quadrilateral $PQRS$ is now formed so that PR is a diagonal, $\angle PRS = 48^\circ$ and $PS = 16$ cm.

Calculate the two possible values of $\angle PSR$.

[3 marks]

*Sebuah segi empat selari $PQRS$ dibentuk dengan PR sebagai pepenjuru, $\angle PRS = 48^\circ$ dan $PS = 16$ cm.**Hitungkan dua nilai $\angle PSR$ yang mungkin.*

- (c) By using the acute $\angle PSR$ from (b), calculate

Dengan menggunakan sudut tirus $\angle PSR$ dari (b), hitungkan

- i. The length, in cm, of RS

Panjang, dalam cm, RS

- ii. The area, in cm^2 , of quadrilateral $PQRS$.

[5 marks]

Luas, dalam cm^2 , segi empat selari $PQRS$

13. The table 3 shows the price indices and percentage of usage of four items, P , Q , R and S , which are the main ingredients in the production of a type of biscuits.

Jadual 3 menunjukkan indeks harga dan peratus penggunaan empat barang P , Q , R dan S , yang menjadi bahan utama dalam penghasilan sejenis biskut.

Items	Price Index for the year 2008 based on the year 2006	Percentage of usage (%)
P	125	30
Q	120	10
R	X	20
S	115	40

Table 3

(a) Calculate

*Hitungkan*i. The price of item P in the year 2006 if the price in the year 2008 was RM 32.*Harga P pada tahun 2006 jika harganya pada tahun 2008 ialah RM 32*ii. The price index of item S in the year 2008 based on the year 2004 if its price index in the year 2006 based on the year 2004 is 140. [5 marks]*Indeks harga S pada tahun 2008 berdasarkan tahun 2004 jika indeks harganya pada tahun 2006 berdasarkan tahun 2004 ialah 140*

(b) The composite index of the cost of biscuits production for the year 2008 based on the year 2006 is 124.5.

Nombor indeks gubahan kos penghasilan biskut itu pada tahun 2008 berdasarkan tahun 2006 ialah 124.5.

Calculate

*Hitungkan*i. The value of x .*Nilai x*

ii. The price of a box of biscuits in the year 2008 if the corresponding price in the year 2006 was RM 14. [5 marks]

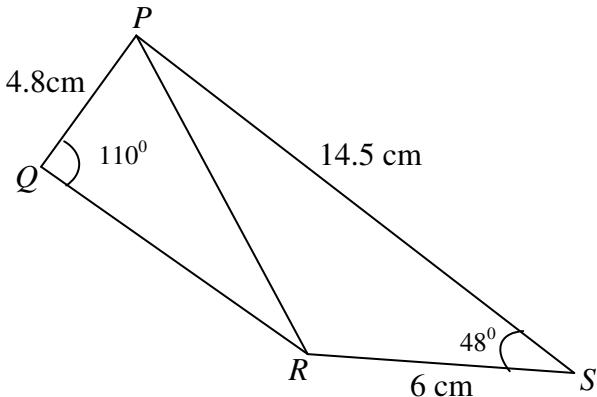
*Harga sekotak biskut itu pada tahun 2008 jika harga yang sepadan pada tahun 2006 ialah RM 14.*14. The diagram 5 shows a quadrilateral $PQRS$ *Rajah 5 menunjukkan segi empat selari $PQRS$* 

Diagram 5

(a) Calculate

Hitungkan(i) The length, in cm, of PR .*Panjang, dalam cm, PR* (ii) $\angle PRQ$. [4 marks](b) Points P' lies on PR such that $P'Q = PQ$ *Titik P' bergerak sepanjang PR dengan keadaan $P'Q = PQ$* (i) Sketch $\Delta P'QR$.*Lakarkan $\Delta P'QR$* (ii) Calculate the area, in cm^2 , of $\Delta P'QR$.

[6 marks]

Hitungkan luas, dalam cm^2 , $\Delta P'QR$

15. The table 4 shows the price indices for four ingredients, A , B , C and D , used in making biscuits of the particular kind. The diagram 6 shows a pie chart which represents the relative amount of the ingredients A , B , C and D , used in making these biscuits.

Jadual 4 menunjukkan harga dan indeks harga empat bahan A , B , C dan D , yang digunakan untuk membuat sejenis biskut. Rajah 6 ialah carta pai yang mewakili kuantiti relatif bagi penggunaan bahan-bahan A , B , C dan D dalam pembuatan biskut itu.

Ingredients	Price per kg (RM)		Price Index for the year 2004 based on the year 2000
	Year 2000	Year 2004	
A	0.80	1.00	x
B	1.60	y	130
C	0.75	1.20	160
D	z	0.90	125

Table 4

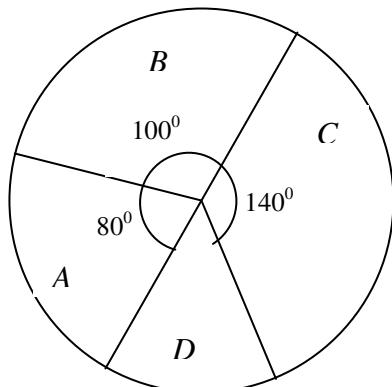


Diagram 6

- (a) Find the value of x , y and z [2 marks]
Carikan nilai x , y dan z
- (b) (i) Calculate the composite index for the cost of making these biscuits in the year 2004 based on the year 2000.
Hitungkan nombor indeks gubahan bagi kos membuat biskut itu pada tahun 2004 berdasarkan tahun 2000.
- (ii) Hence, calculate the corresponding cost of making these biscuits in the year 2000 if the cost in the year 2004 was RM 28.50. [5 marks]
Seterusnya, hitungkan kos membuat biskut yang sepadan bagi tahun 2000 jika kos membuatnya pada tahun 2004 ialah RM 28.50
- (c) The cost of making these biscuits is expected to increase by 30% from the year 2004 to the year 2008. Find the expected composite index for the year 2008 based on the year 2000. [3 marks]
Kos membuat biskut itu dijangka meningkat sebanyak 30% dari tahun 2004 ke tahun 2008.
Carikan nombor indeks gubahan bagi kos membuat biskut itu yang dijangkakan pada tahun 2008 berdasarkan tahun 2000.

END OF QUESTIONS

**SULIT
3472/2
Additional
Mathematics
Paper 2
2009**

**PEJABAT PENDIDIKAN DAERAH
JASIN * ALOR GAJAH * MELAKA TENGAH
JABATAN PENDIDIKAN MELAKA
KEMENTERIAN PELAJARAN MALAYSIA**

**PEPERIKSAAN AKHIR TAHUN
TINGKATAN 4**

2009

ADDITIONAL MATHEMATICS

Paper 2

MARKING SCHEME

This marking scheme consists of 10 printed pages

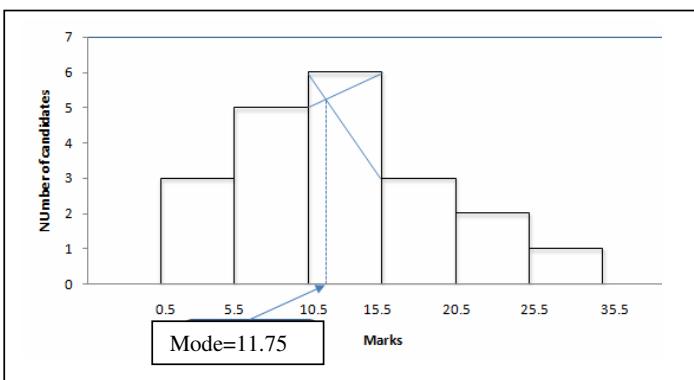
ANSWER SCHEME PAPER 2

Number	Solutions	S M	F M
1	$x = 8 - y$ $(8 - y)^2 - 6y + y^2 = 16$ $y^2 - 11y + 24 = 0$ $(y - 8)(y - 3) = 0$ $y = 3, y = 8$ when $y = 3, x = 5 : (5, 3)$ when $y = 8, x = 0 : (0, 8)$	1 1 1 1 1	5
2 (a)	Let $f^{-1}(x) = y$ $f(y) = x$ $2y - 1 = x$ $y = \frac{x+1}{2}$ $\therefore f^{-1}(x) = \frac{x+1}{2}$		
(b)	$f^{-1}g(x) = f^{-1}\left(\frac{x}{3} + 1\right)$ $= \frac{\left(\frac{x}{3} + 1\right) + 1}{2}$ $= \frac{x}{6} + 1$	1 1 1	1 2
(c)	$h[g(x)] = 3x + 6$ $h\left(\frac{x}{3} + 1\right) = 3x + 6$ Let $z = \frac{x}{3} + 1$ $\therefore x = 3(z - 1)$ $\therefore h(z) = 3(3(z - 1)) + 6$ $\therefore h(x) = 9x - 3$	1 1 1	
3 (a)	$2^x \cdot 2^3 - 2^x \cdot 2^2 = 2$ $2^x = 2^{-1}$ or $x + 2 = 1$ $x = -1$	1 1 1	3

(b)	$\log_9(x+9) = 3 \log_9 5$ $\log_9(x+9) = \log_9 5^3$ $\therefore (x+9) = 5^3$ $x = 125 - 9$ $x = 116$	1 1 1	3
4(a)	$35 \frac{1}{3} = 29.5 + \left(\frac{\frac{28+x-13}{2}}{x} \right) 10$ $x = 12$	P1 (29.5) K1 N1	3
(b)	$\sum f_x = 1390$ $\bar{x} = \frac{1390}{40}$ $= 34.75$	P1 K1 N1	3
5(a)	$\frac{dy}{dx} = 2x - 8$ $2x - 8 = 0$ $(4, -12)$	K1 K1 N1	3
(b)	$\frac{d^2y}{dx^2} = 2$ $(x^2 - 8x + 4)(2) + x(2x - 8) + 12 = 0$ $(x-1)(x-5) = 0$ $x = 1, x = 5$	P1 K1 K1 N1	4
6(a)	$y = x - 4k - 2$ or $kx^2 - 2kx - 3k = 0$ $kx^2 - 2kx - 3k = x - 4k - 2$ $(-2k-1)^2 - 4(k)(k+2) < 0$ $-4k+1 < 0$ $k > \frac{1}{4}$	P1 K1 K1 K1 N1	5
(b)	$(x-3h)^2 - 9h^2 + 8h^2 + 1$ $-h^2 + 1 = t + 2h^2$ $t = 1 - 3h^2$	K1 K1 N1	3

Comment [U1]:

7	<p>(a) Midpoint of QR = (5,4) or $m_{QR} = 1$ $y = -x + c$ passes through (5,4) $y = -x + 9$ or equivalent</p> <p>or</p> <p>$\sqrt{(x-6)^2 + (y-5)^2}$ or $\sqrt{(x-4)^2 + (y-3)^2}$</p> $x^2 - 12x + 36 + y^2 - 10y + 25 = x^2 - 8x + 16 + y^2 - 6y + 9$ $y = -x + 9$ or equivalent <p>(b) $\sqrt{(x-4)^2 + (y-3)^2} = 2$</p> $x^2 + y^2 - 8x - 6y + 21 = 0$ <p>(c) $x^2 + (9-x)^2 - 8x - 6(9-x) + 21 = 0$</p> $(x-4)(x-6) = 0$ $(4,5), (6,3)$ <p>(d) Replacing point (5,4) to equation of locus P. No</p>	<p>1 1 1</p> <p>1 1 1</p> <p>1 1 1</p> <p>1 1 1</p> <p>1 1 1</p>
8	<p>(a) $h = \frac{24}{x^2}$ or curved surface area of cone = $2\pi x^2$ or curved surface area of cylinder = $2\pi x(\frac{24}{x^2})$</p> <p>Total surface area = $2\pi x^2 + 2\pi x(\frac{24}{x^2}) + \pi x^2$ $= 3\pi(x^2 + \frac{16}{x})$</p> <p>(b) $6\pi x - \frac{48\pi}{x^2} = 0$</p> $x = 2$ $A = 36\pi$ <p>(c) $\frac{dx}{dt} = \frac{dx}{dA} \times \frac{dA}{dt}$ $= \frac{1}{6\pi x - \frac{48\pi}{x^2}} (42\pi)$ $= 2$</p>	<p>1 1 1</p> <p>1 1 1</p> <p>1 1 1</p>

	(d) $\delta A = (6\pi x - \frac{48\pi}{x^2})(0.003)$ = 0.063π	1 1	2
9	(a) Identify Q_1 class = 6 – 10 or $L = 5.5$ $5.5 + \left[\frac{\frac{1}{4}(17+k)-3}{5} \right] (5) = 7.5$ $k = 3$ (b) $\bar{x} = \frac{255}{20}$ or $\sum x^2 = 4175$ $\delta = \sqrt{\frac{4175}{20} - \left(\frac{255}{20}\right)^2}$ $= 6.796$ (c) Complete histogram Using X to determine the mode Mode = 11.75	1 1 1 1 1 1 2 1 1	3 3 3 3 3 4
10	 (a) 60° (b) $s = 8(20 \times \frac{\pi}{180})$ $= 2.973 \text{ cm}$ (c) $AB^2 = 8^2 + 8^2 - 2(8)(8)\cos 100$ $AB = 12.26 \text{ cm}$ Perimeter = 26.21 cm	1 1 1 1 1	1 2 3

	(d) Segment 1 = $\frac{1}{2} (8^2)(1.745) - \frac{1}{2} (8)(8) \sin 100$ Segment 2 = $\frac{1}{2} (8^2)(1.047) - \frac{1}{2} (8)(8) \sin 60$ Shaded region = $24.33 - 5.791$ = 18.54 cm^2	1 1 1 1	4
11	(a) $m_{AC} = 2$ or $m_{AB} = -\frac{1}{2}$ $m_{AC}^* \times m_{AB}^* = -1$	1 1	2
	(b) midpoint $AC = (0, 0)$ $D(x, y) = \left(\frac{x+7}{2}, \frac{y-1}{2} \right)$ $\frac{x+7}{2} = 0$ or $\frac{y-1}{2} = 0$ $x = -7$ or $y = 1$ $D = (-7, 1)$	1 1	2
	Area of parallelogram = $\frac{1}{2} \begin{vmatrix} 1 & 7 & -1 & -7 \\ 2 & -1 & -2 & 1 \end{vmatrix}$ = $\frac{1}{2} 29 - 16 ^*$ = $\frac{13}{2} \text{ unit}^2$	1 1	2
	(c) Centre = midpoint BC = $E(3, -\frac{3}{2})$	1	
	Distance EC or Distance EB or Distance ED $\sqrt{(x-3)^2 + \left(y + \frac{3}{2}\right)^2} = \sqrt{(3+1)^2 + \left(-\frac{3}{2} + 2\right)^2}$ or	1	
	$\sqrt{(x-3)^2 + \left(y + \frac{3}{2}\right)^2} = \sqrt{(7-3)^2 + \left(-1 + \frac{3}{2}\right)^2}$ $x^2 + y^2 - 6x + 3y - 5 = 0$	1 1	4

	<p>i) $\sum IW = 9550 + 20x$</p> <p>Use $\bar{I}_{08/06} = \frac{\sum IW}{100} *$</p> $124.5 = \frac{9550 + 20x}{100}$ $x = 145$ <p>ii) Use $\bar{I}_{08/06} = \frac{\text{Cost}_{08}}{\text{Cost}_{06}} \times 100$ or equivalent</p> <p>or $\text{Cost}_{08} = \frac{\text{RM}124.5 \times 14}{100}$</p> $= \text{RM} 17.43$	1 1 1 1 1	5
14	<p>(a) i) $PR^2 = 6^2 + 14.5^2 - 2(6)(14.5) \cos 48^\circ$</p> $PR = 11.39 \quad (\text{at least 3 s.f, correct round off})$ <p>ii) $\frac{\sin PRQ}{4.8} = \frac{\sin 110^\circ}{11.39 *}$ or equivalent</p> $S = 23.33^\circ$ <p>(must 2 d.p, correct round off, decimal form better than minutes form)</p>	1 1 1 1	4
	<p>(b) i)</p> <p><i>Must correct labeled, angle P' is obtuse</i></p> <p>ii) $P = 180 - 110^\circ - 23.33^\circ$</p> $= 46.67^\circ$	1 1	

	$\frac{QR}{\sin 46.67^*} = \frac{QR}{\sin 133.33^*} = \frac{4.8}{\sin 23.33^*}$ $QR = 8.817 / 8.82$ $\angle P'QR = 180^0 - 133.33^0 - 23.33^0$ $= 23.34^0$ $\text{Area } P'QR = \frac{1}{2} \times (4.8)(8.82^*) \times \sin 23.34^0$ $= 8.386$	1 1 1 1 6																								
15	<p>(a) Use $I_{04/00} = \frac{P_{04}}{P_{00}} \times 100$ $x = 125, y = 2.08, z = 0.72$</p> <p>(b) i)</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <thead> <tr> <th>Item</th> <th>I</th> <th>W</th> <th>IW</th> </tr> </thead> <tbody> <tr> <td>A</td> <td>125*</td> <td>80</td> <td>10000*</td> </tr> <tr> <td>B</td> <td>130</td> <td>100</td> <td>13000</td> </tr> <tr> <td>C</td> <td>160</td> <td>140</td> <td>22400</td> </tr> <tr> <td>D</td> <td>125</td> <td>40</td> <td>5000</td> </tr> <tr> <td></td> <td></td> <td>$\sum W = 360$</td> <td>$\sum IW = 50400$</td> </tr> </tbody> </table> <p>$\sum IW = 50400$</p> <p>Use $\bar{I}_{04/00} = \frac{\sum IW}{360}$ or</p> $\bar{I}_{04/00} = \frac{50400^*}{360}$ $= 140$ <p>ii) Use $\bar{I}_{04/00} = \frac{\text{Cost}_{04}}{\text{Cost}_{00}} \times 100$ or</p> $\text{Cost}_{00} = \frac{\text{RM}128.50 \times 100}{140}$ $= \text{RM}20.36$	Item	I	W	IW	A	125*	80	10000*	B	130	100	13000	C	160	140	22400	D	125	40	5000			$\sum W = 360$	$\sum IW = 50400$	1 1 1 1 5
Item	I	W	IW																							
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C	160	140	22400																							
D	125	40	5000																							
		$\sum W = 360$	$\sum IW = 50400$																							

	(c) $\bar{I}_{08/04} = 130$ Use $I_{08/04} = \frac{I_{08/04} \times I_{04/00}}{100}$ or $= \frac{130 \times 140}{100}$ $= 182$	1	
		1	3