

Name : .....

Form : .....



**KEMENTERIAN  
PENDIDIKAN  
MALAYSIA**

**BAHAGIAN PENGURUSAN SEKOLAH BERASRAMA PENUH  
DAN SEKOLAH KECEMERLANGAN**

**PENTAKSIRAN DIAGNOSTIK AKADEMIK SBP 2014  
PERCUBAAN SIJIL PELAJARAN MALAYSIA**

**ADDITIONAL MATHEMATICS**

**Kertas 1**

**1 jam 15 minit**

**JANGAN BUKA KERTAS SOALANINI  
SEHINGGA DIBERITAHU**

1. *Tulis nama dan tingkatan anda pada ruangan yang disediakan.*
2. *Kertas soalan ini adalah dalam dwibahasa.*
3. *Soalan dalam bahasa Inggeris mendahului soalan yang sepadan dalam bahasa Melayu.*
4. *Calon dibenarkan menjawab keseluruhan atau sebahagian soalan sama ada dalam bahasa Inggeris atau bahasa Melayu.*
5. *Calon dikehendaki membaca maklumat di halaman belakang kertas soalan ini.*

<i>Untuk Kegunaan Pemeriksa</i>		
Soalan	Markah Penuh	Markah Diperolehi
1	2	
2	3	
3	3	
4	3	
5	3	
6	3	
7	3	
8	4	
9	3	
10	3	
11	4	
12	3	
13	3	
14	4	
15	2	
16	4	
17	4	
18	3	
19	3	
20	3	
21	3	
22	3	
23	3	
24	4	
25	4	
<b>TOTAL</b>	<b>80</b>	

Kertas soalan ini mengandungi **26** halaman bercetak.

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***HALAMAN KOSONG***

The following formulae may be helpful in answering the questions. The symbols given are the ones commonly used.

**ALGEBRA**

$$1 \quad x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$2 \quad a^m \times a^n = a^{m+n}$$

$$3 \quad a^m \div a^n = a^{m-n}$$

$$4 \quad (a^m)^n = a^{nm}$$

$$5 \quad \log_a mn = \log_a m + \log_a n$$

$$6 \quad \log_a \frac{m}{n} = \log_a m - \log_a n$$

$$7 \quad \log_a m^n = n \log_a m$$

$$8 \quad \log_a b : \begin{array}{c} \text{loge } b \\ \hline - \end{array}$$

$$9 \quad T_n = a + (n-1)d$$

$$10 \quad S_n = \frac{n}{2}[2a + (n-1)d]$$

$$11 \quad T_n = ar^{n-1}$$

$$12 \quad S_{\infty} = \frac{a(r^n - 1)}{r-1} = \frac{a(1 - r^n)}{1-r}, \quad (r \neq 1)$$

$$13 \quad S_{\infty} = \frac{a}{1-r}, \quad |r| < 1$$

**CALCULUS**

$$1 \quad y = uv, \quad \frac{dy}{dx} = u \frac{dv}{dx} + v \frac{du}{dx}$$

$$2 \quad y = \frac{u}{v}, \quad \frac{dy}{dx} = \frac{v \frac{du}{dx} - u \frac{dv}{dx}}{v^2},$$

$$3 \quad \frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx}$$

$$4 \quad \text{Area under a curve}$$

$$= \int_a^b y \, dx \quad \text{or}$$

$$= \int_a^b x \, dy$$

$$5 \quad \text{Volume generated}$$

$$= \int_a^b \pi y^2 \, dx \quad \text{or}$$

$$= \int_a^b \pi x^2 \, dy$$

**GEOMETRY**

$$1 \quad \text{Distance} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$2 \quad \text{Midpoint}$$

$$(x, y) = \left( \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

$$3 \quad |r| = \sqrt{x^2 + y^2}$$

$$4 \quad \hat{r} = \frac{xi + yj}{\sqrt{x^2 + y^2}}$$

$$5 \quad \text{A point dividing a segment of a line}$$

$$(x, y) = \left( \frac{nx_1 + mx_2}{m+n}, \frac{ny_1 + my_2}{m+n} \right)$$

$$6 \quad \text{Area of triangle} =$$

$$\frac{1}{2} |(x_1y_2 + x_2y_3 + x_3y_1) - (x_2y_1 + x_3y_2 + x_1y_3)|$$

**[Lihat halaman sebelah**

## STATISTIC

$$1 \quad \bar{x} = \frac{\sum x}{N}$$

$$2 \quad \bar{x} = \frac{\sum fx}{\sum f}$$

$$3 \quad \sigma = \sqrt{\frac{\sum(x - \bar{x})^2}{N}} = \sqrt{\frac{\sum x^2}{N} - \bar{x}^2}$$

$$4 \quad \sigma = \sqrt{\frac{\sum f(x - \bar{x})^2}{\sum f}} = \sqrt{\frac{\sum fx^2}{\sum f} - \bar{x}^2}$$

$$5 \quad m = L + \left[ \frac{\frac{1}{2}N - F}{f_m} \right] C$$

$$6 \quad I = \frac{Q_1}{Q_0} \times 100$$

$$7 \quad \bar{I} = \frac{\sum w_i I_i}{\sum w_i}$$

$$8 \quad {}^n P_r = \frac{n!}{(n-r)!}$$

$$9 \quad {}^n C_r = \frac{n!}{(n-r)!r!}$$

$$10 \quad P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$11 \quad P(X = r) = {}^n C_r p^r q^{n-r}, \quad p + q = 1$$

$$12 \quad \text{Mean } \mu = np$$

$$13 \quad \sigma = \sqrt{npq}$$

$$14 \quad z = \frac{x - \mu}{\sigma}$$

## TRIGONOMETRY

$$1 \quad \text{Arc length, } s = r\theta$$

$$9 \quad \sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$$

$$2 \quad \text{Area of sector, } L = \frac{1}{2}r^2\theta$$

$$10 \quad \cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$$

$$3 \quad \sin^2 A + \cos^2 A = 1$$

$$11 \quad \tan(A \pm B) = \frac{\tan A \pm \tan B}{1 \mp \tan A \tan B}$$

$$4 \quad \sec^2 A = 1 + \tan^2 A$$

$$12 \quad \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$6 \quad \sin 2A = 2 \sin A \cos A$$

$$13 \quad a^2 = b^2 + c^2 - 2bc \cos A$$

$$7 \quad \cos 2A = \cos^2 A - \sin^2 A \\ = 2 \cos^2 A - 1 \\ = 1 - 2 \sin^2 A$$

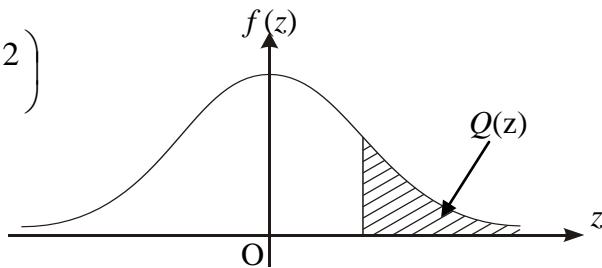
$$14 \quad \text{Area of triangle} = \frac{1}{2}ab \sin C$$

$$8 \quad \tan 2A = \frac{2 \tan A}{1 - \tan^2 A}$$

## THE UPPER TAIL PROBABILITY $Q(z)$ FOR THE NORMAL DISTRIBUTION $N(0,1)$ KEBARANGKALIAN HUJUNG ATAS $Q(z)$ BAGI TABURAN NORMAL $N(0, 1)$

$$f(z) = \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{1}{2}z^2\right)$$

$$Q(z) = \int_k^{\infty} f(z) dz$$

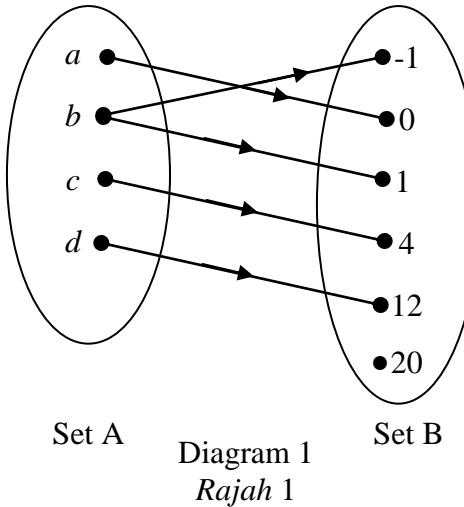


### **Example / Contoh:**

If  $X \sim N(0, 1)$ , then  $P(X > k) = Q(k)$   
*Jika*  $X \sim N(0, 1)$ , maka  $P(X > k) = Q(k)$

Answer **all** questions.  
*Jawab semua soalan.*

1. Diagram 1 shows the relation between set A and set B.  
*Rajah 1 menunjukkan hubungan antara set A dan set B.*



- (a) State the range of the relation.  
*Nyatakan julat bagi hubungan itu.*
- (b) The relation is not a function. Give your reason.  
*Hubungan itu bukan suatu fungsi. Beri sebab anda.*

[ 2 marks ]  
[2 markah]

*Answer/Jawapan :*

(a)

(b)

1

2

2. The function  $h$  is defined as  $h^{-1}(x) = \frac{7x}{x-3}, x \neq m$ .

*Fungsi  $h$  ditakrifkan oleh  $h^{-1}(x) = \frac{7x}{x-3}, x \neq m$ .*

Find

Cari

- (a) the value of  $m$

*nilai bagi  $m$*

- (b)  $h(6)$

[ 3 marks ]  
[3 markah]

Answer/Jawapan :

(a)

(b)

2

3

- 3 The following information refers to the functions  $g$  and  $fg$ .

*Maklumat berikut adalah berkaitan dengan fungsi  $g$  dan  $fg$ .*

$g(x) = 3x - 1$
$fg(x) = 6x + 8$

Find  $f(x)$ .

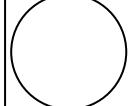
Cari  $f(x)$ .

[ 3 marks ]  
[3 markah]

Answer/Jawapan :

3

3



For  
Examiner's  
Use

4. Given that  $m$  and  $n$  are the roots of quadratic equations  $x^2 + 6x + 7 = 0$ , form the quadratic equation which has the roots  $4m$  and  $4n$ .

*Diberi bahawa  $m$  dan  $n$  adalah punca-punca bagi persamaan kuadratik  $x^2 + 6x + 7 = 0$ , bentukkan persamaan kuadratik yang mempunyai punca-punca  $4m$  dan  $4n$ .*

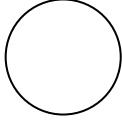
[ 3 marks ]

[3 markah]

Answer/Jawapan : \_\_\_\_\_

4

3



5. Diagram 5 shows the graph of quadratic function  $f(x) = -\frac{1}{3}[(x+p)^2 + q]$

The straight line  $y = 3$  is a tangent to the curve.

Rajah 5 menunjukkan suatu graf fungsi kuadratik  $f(x) = -\frac{1}{3}[(x+p)^2 + q]$

Garis lurus  $y = 3$  ialah tangen kepada lengkung tersebut.

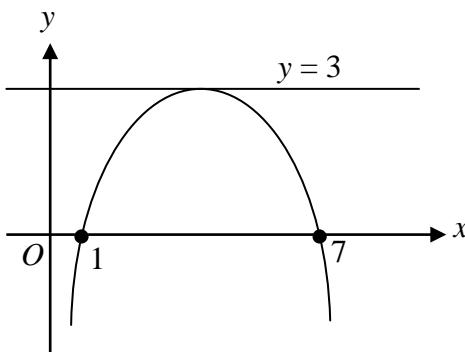


Diagram 5  
Rajah 5

Calculate the value of  $p$  and of  $q$ .

Hitung nilai bagi  $p$  dan bagi  $q$ .

[3 marks]

[3 markah]

Answer/Jawapan : \_\_\_\_\_

5

3

For  
Examiner's  
Use

- 6 Given that  $h(x) = 10 - x - 2x^2$ .

Find the range of values of  $x$  for  $h(x) \geq 4$ .

Diberi bahawa  $h(x) = 10 - x - 2x^2$ .

Cari julat nilai-nilai  $x$  untuk  $h(x) \geq 4$ .

[3 marks]

[3 markah]

Answer/Jawapan :

**6**

3

7. Given that  $4(2^{p+1}) = \left(\frac{1}{8}\right)^{2p+6}$ , find the value of  $p$ .

Diberi  $4(2^{p+1}) = \left(\frac{1}{8}\right)^{2p+6}$ , cari nilai  $p$ .

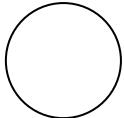
[ 3 marks ]

[3 markah]

Answer/Jawapan :

**7**

3



8. Solve the equation

*Selesaikan persamaan*

$$\log_3(2x-5) = \log_{27}(x+1)^3$$

[ 4 marks ]

[4 markah]

*Answer/Jawapan :*

8

4

9. If the  $n^{th}$  term of an arithmetic progression is  $4n + 3$ , find the sum of the first 20 terms.

*Jika sebutan ke-n bagi suatu janjang aritmetik adalah  $4n+3$ , cari hasil tambah 20 sebutan pertama.*

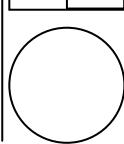
[ 3 marks ]

[3 markah]

*Answer/Jawapan :*

9

3

- 10 In the year 2013 the price of a hand phone decrease 5% each month. Diagram 10 shows the price of a hand phone in January 2013.

*Pada tahun 2013 harga sebuah telefon bimbit menyusut 5% setiap bulan. Rajah 10 menunjukkan harga sebuah telefon bimbit pada bulan Januari tahun 2013.*



Diagram 10  
*Rajah 10*

David bought a new hand phone a day before Christmas for his mother.

*David telah membeli sebuah telefon bimbit baru sehari sebelum Hari Natal untuk dihadiahkan kepada ibunya.*

How much David pay for the new handphone?

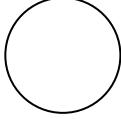
*Berapakah harga yang telah dibayar oleh David untuk membeli telefon baru tersebut?*

[ 3 marks ]  
[3 markah]

Answer/Jawapan : \_\_\_\_\_

10

3



- 11 The sum of the first 8 terms of an arithmetic progression is 192 and the sum of the next 8 terms is 448.

*Hasiltambah 8 sebutan pertama bagi suatu janjang aritmetik adalah 192 dan hasiltambah 8 sebutan yang berikutnya adalah 448.*

Calculate the values of the first term and the common different.

*Hitung sebutan pertama dan beza sepunya.*

[ 4 marks ]  
[4 markah]

Answer/Jawapan : \_\_\_\_\_

11

4

- 12 Diagram 12 shows a straight line graph of  $\frac{1}{y}$  against  $\frac{1}{x}$ .

Express  $y$  in terms of  $x$ .

Rajah 12 menunjukkan graf garislurus  $\frac{1}{y}$  melawan  $\frac{1}{x}$ .

Ungkapkan  $y$  dalam sebutan  $x$ .

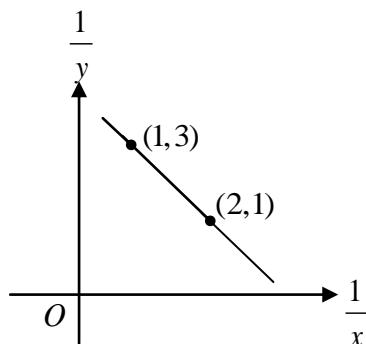


Diagram 12  
Rajah 12

[ 3 marks ]  
[3 markah]

Answer/Jawapan :

12

3

13.

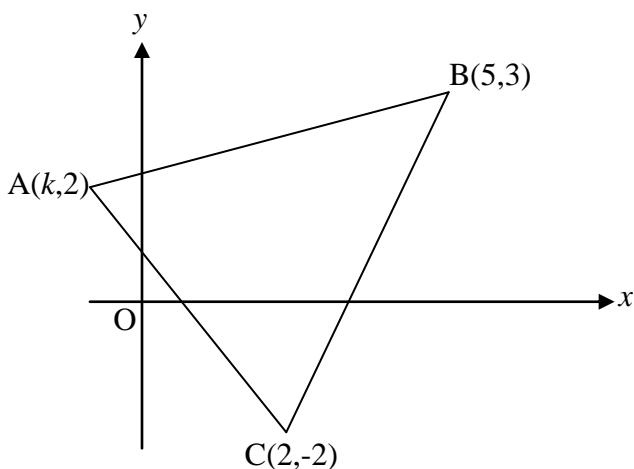


Diagram 13  
Rajah 13

Diagram 13 shows the triangle  $ABC$ . Given that the area of the triangle is  $13.5 \text{ unit}^2$ , find the value of  $k$ .

*Rajah 13 menunjukkan segitiga  $ABC$ . Diberi luas segitiga itu ialah  $13.5 \text{ unit}^2$ , cari nilai bagi  $k$ .*

[3 marks]  
[3 markah]

Answer/Jawapan:

13

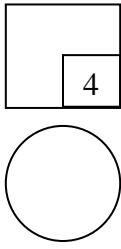
3

14. Given that  $M(6,4)$  is the midpoint of the line segment that joins the point  $P(4,8)$  and point  $R$ . Find the equation of the straight line that passes through the point  $R$  and is perpendicular to the straight line  $PR$ .

*Diberi bahawa  $M(6,4)$  adalah titik tengah tembereng garis yang menghubungkan titik  $P(4,8)$  dan titik  $R$ . Cari persamaan garislurus yang melalui titik  $R$  dan berserenjang dengan garislurus  $PR$ .*

[4 marks]  
[4 markah]

Answer/Jawapan : \_\_\_\_\_

**14**

15. Diagram 15 shows the vector  $\overrightarrow{OP}$ ,  $\overrightarrow{OR}$  and  $\overrightarrow{OQ}$  drawn on a grid of equal squares with sides of 1 unit.

*Rajah 15 menunjukkan vector  $\overrightarrow{OP}$ ,  $\overrightarrow{OR}$  dan  $\overrightarrow{OQ}$  dilukis pada grid segiempat sama yang sama besar bersisi 1 unit.*

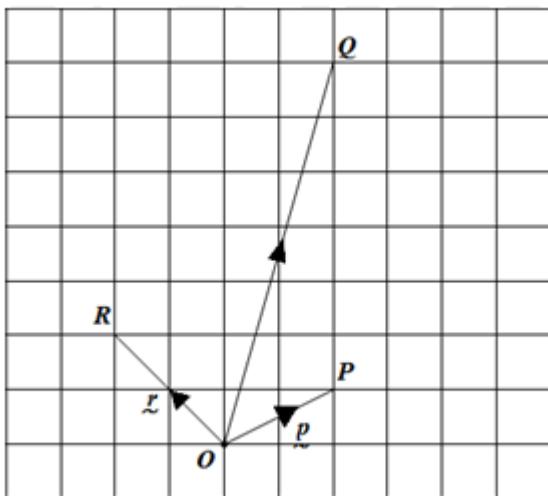


Diagram 15  
Rajah 15

Determine  
*Tentukan*

- (a)  $\overrightarrow{OQ}$  in terms of  $\overrightarrow{p}$  and  $\overrightarrow{r}$ .  
(b)  $|\overrightarrow{OQ}|$

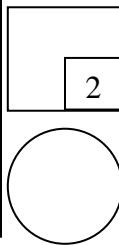
[2 marks]  
[2 markah]

Answer/Jawapan : :

(a)

(b)

15



16. It is given that  $\underline{a} = \begin{pmatrix} 1 \\ 3 \end{pmatrix}$  and  $\underline{b} = \begin{pmatrix} 2 \\ h+1 \end{pmatrix}$ . If  $\underline{a}$  is parallel to  $\underline{b}$ , find

Diberi bahawa  $\underline{a} = \begin{pmatrix} 1 \\ 3 \end{pmatrix}$  dan  $\underline{b} = \begin{pmatrix} 2 \\ h+1 \end{pmatrix}$ . Jika  $\underline{a}$  selari dengan  $\underline{b}$ , cari

- (a) the value of  $h$

nilai bagi  $h$

- (b) the unit vector in the direction of  $\underline{b}$ .

vector unit dalam arah  $\underline{b}$ .

[4 marks]

[4 markah]

Answer/Jawapan :

(a)

(b)

17.

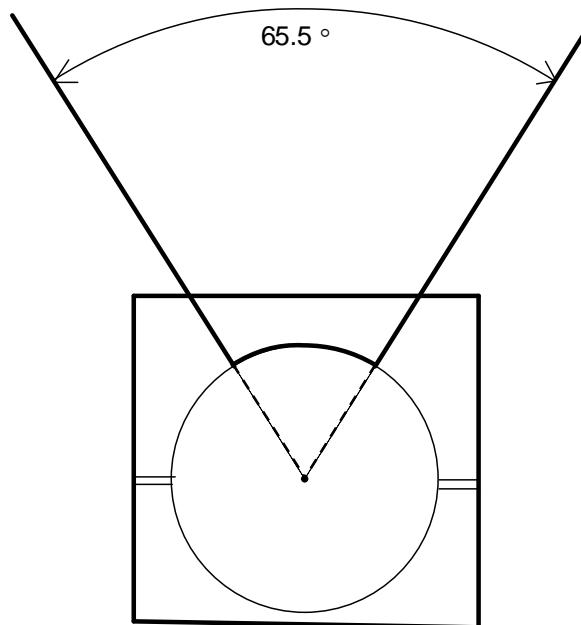


Diagram 17  
*Rajah 17*

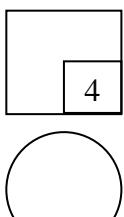
Diagram 17 shows shot pull field dimension for high school. For category A, student must throw 5 m far from centre to get 1 point and 7 m far from centre for 3 points. Find the area, in  $\text{m}^2$  for 1 point.

*Rajah 17 menunjukkan dimensi ukuran padang lontar peluru bagi sekolah menengah. Bagi kategori A, pelajar mesti mendapat jarak 5 m dari pusat balingan untuk 1 mata dan 7 m dari pusat balingan untuk 3 mata. Cari luas kawasan, dalam  $\text{m}^2$ , untuk 1 mata.*

[4 marks]  
[4 markah]

Answer/Jawapan :

17



For  
Examiner's  
Use

18. Given  $\sin \theta = \sqrt{1 - h^2}$  and  $\theta$  is obtuse angle.  
*Diberi*  $\sin \theta = \sqrt{1 - h^2}$  dan  $\theta$  ialah sudut cakah.

Find

*Cari*

(a)  $\cot \theta$

(b)  $\sin 2\theta$

[ 3 marks ]

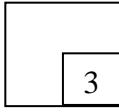
[3 markah]

Answer/Jawapan :

(a)

(b)

18



3

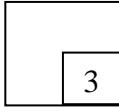
19. Given  $y = \frac{3x^2 - 4}{x}$  and  $\frac{dy}{dx} = 3h(x)$ , find  $\int_{-2}^1 h(x)dx$   
*Diberi*  $y = \frac{3x^2 - 4}{x}$  dan  $\frac{dy}{dx} = 3h(x)$ , cari  $\int_{-2}^1 h(x)dx$

[ 3 marks ]

[3 markah]

Answer/Jawapan :

19



3

For  
Examiner's  
Use

20. Given  $y = 3x^2 - 4x + 5$ , find

Diberi  $y = 3x^2 - 4x + 5$ , cari

- (a) the value of  $x$  when  $y$  is minimum.  
*nilai x apabila nilai y adalah minimum*
- (b) the minimum value of  $y$ .  
*nilai minimum bagi y.*

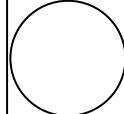
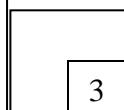
[ 3 marks ]  
[3 markah]

Answer/Jawapan :

(a)

(b)

20



21. Given that  $\int_1^3 h(x)dx = 5$ , find the value of  $k$ , if  $\int_1^3 kx dx - \int_1^3 2h(x)dx = 18$

*Diberi bahawa  $\int_1^3 h(x)dx = 5$ , cari nilai  $k$ , jika  $\int_1^3 kx dx - \int_1^3 2h(x)dx = 18$*

[ 3 marks ]  
[3 markah]

Answer/Jawapan :

21

3

22. The mean and standard deviation of five numbers are 6 and 3 respectively.

*Min dan sisihan piawai bagi lima nombor adalah 6 dan 3 masing-masing.*

Find

Cari

- (a) the sum of squares of the numbers.

*hasil tambah kuasadua bagi nombor-nombor tersebut.*

- (b) the new value of variance if every number is multiplied by 2 and then 3 is added to it.

*nilai varian yang baru jika setiap nombor didarab dengan 2 dan kemudian 3 ditambah kepadanya.*

[ 3 marks ]  
[3 markah]

Answer/Jawapan :

(a)

22

3

(b)

23. En. Lee has a pets shop. He want to display five cages with different pets as shown in Diagram 23.

*En. Lee mempunyai sebuah kedai binatang peliharaan. Di hadapan kedainya dipamerkan lima sangkar yang diisi dengan haiwan yang berbeza seperti pada Rajah 23.*

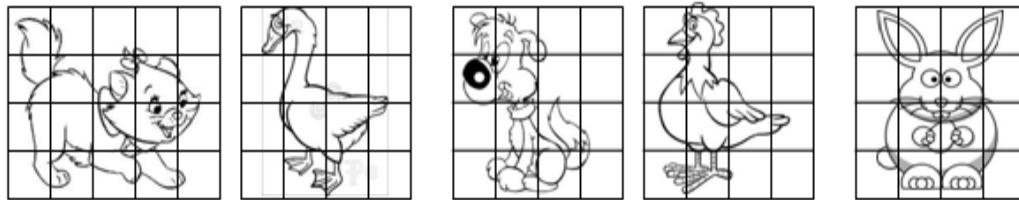


Diagram 23  
Rajah 23

Cat and dog cage's cannot be side by side.

*Sangkar anjing dan sangkar kucing tidak boleh bersebelahan.*

How many ways to arrange the cages?

*Berapakah bilangan cara untuk menyusun sangkar-sangkar tersebut?*

[ 3 marks ]  
[3 markah]

Answer/Jawapan : \_\_\_\_\_

23

3

24. Table 24 shows the number of Mathematics and Science books in two racks,  $P$  and  $Q$ .

*Jadual 24 menunjukkan bilangan buku Matematik dan buku Sains di atas dua rak iaitu  $P$  dan  $Q$ .*

Rack <i>Rak</i>	Mathematics book <i>Buku Matematik</i>	Sciences book <i>Buku Sains</i>
$P$	3	$h$
$Q$	5	8

Table 24  
*Jadual 24*

- (a) A book is chosen at random from rack P. The probability of choosing Science book is  $\frac{4}{5}$ .

Find the value of  $h$ .

[2 marks]

*Sebuah buku dipilih secara rawak daripada rak P. Kebarangkalian untuk memilih buku Sains ialah  $\frac{4}{5}$ .*

*Cari nilai  $h$ .*

[2 markah]

- (b) Two books are chosen at random among Mathematics book.

Find the probability that both books are from the same rack.

[2 marks]

*Dua buah buku dipilih secara rawak di kalangan buku Matematik.*

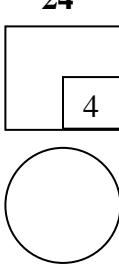
*Cari kebarangkalian bahawa kedua-dua buah buku adalah daripada rak yang sama.*

[2 markah]

Answer/Jawapan :

(a)

(b)



24

25. Diagram 25 shows a standard normal distribution graph.

Rajah 25 menunjukkan graf taburan normal piawai.

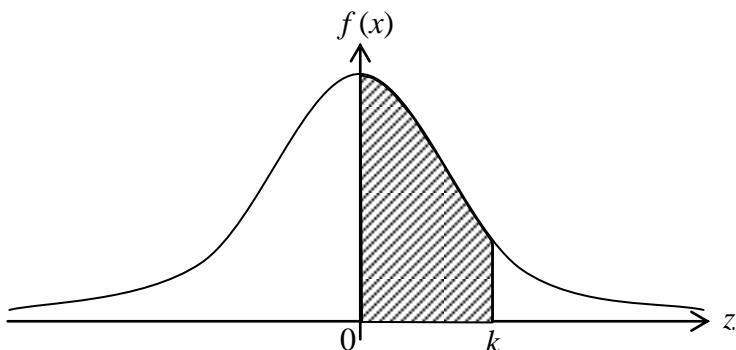


Diagram 25  
Rajah 25

It is given that the area of shaded region is 0.3494.

- (a) Find the value of  $P(z > k)$ .

Cari nilai  $P(z > k)$ .

[ 1 marks ]  
[1 markah]

- (b)  $X$  is a continuous random variable which is normally distributed with a mean of  $\mu$  and a standard deviation of 3.5.

If the value of  $X$  is 56 and the  $z$ -score is  $k$ , find the value of  $\mu$ .

$X$  ialah pembolehubah rawak yang bertabur secara normal dengan min,  $\mu$  dan sisihan piawai 3.5.

Jika nilai  $X$  ialah 56 dan skor-z ialah  $k$ , cari nilai  $\mu$ .

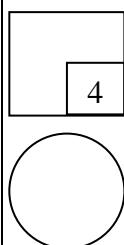
[ 3 marks ]  
[3 markah]

Answer/Jawapan :

(a)

(b)

25



**END OF QUESTION PAPER  
KERTAS SOALAN TAMAT**

**INFORMATION FOR CANDIDATES**  
**MAKLUMAT UNTUK CALON**

1. This question paper consists of **25** questions.  
*Kertas soalan ini mengandungi **25** soalan.*
2. Answer **all** questions.  
*Jawab **semua** soalan.*
3. Write your answers in the spaces provided in the question paper.  
*Tulis jawapan anda dalam ruang yang disediakan dalam kertas soalan.*
4. Show your working. It may help you to get marks.  
*Tunjukkan langkah-langkah penting dalam kerja mengira anda. Ini boleh membantu anda untuk mendapatkan markah.*
5. If you wish to change your answer, cross out the answer that you have done.  
Then write down the new answer.  
*Sekiranya anda hendak menukar jawapan, batalkan jawapan yang telah dibuat. Kemudian tulis jawapan yang baru.*
6. The diagrams in the questions provided are not drawn to scale unless stated.  
*Rajah yang mengiringi soalan tidak dilukis mengikut skala kecuali dinyatakan.*
7. The marks allocated for each question are shown in brackets.  
*Markah yang diperuntukkan bagi setiap soalan ditunjukkan dalam kurungan.*
8. A list of formulae is provided on pages 3 to 5.  
*Satu senarai rumus disediakan di halaman 3 hingga 5.*
9. You may use a non-programmable scientific calculator.  
*Anda dibenarkan menggunakan kalkulator saintifik yang tidak boleh diprogram.*
10. Hand in this question paper to the invigilator at the end of the examination.  
*Serahkan kertas soalan ini kepada pengawas peperiksaan di akhir peperiksaan.*