

3472/1

**Matematik Tambahan
Kertas 1
Mei 2007
2 hours**



3472/1

Name :

Form :

**SEKTOR SEKOLAH BERASRAMA PENUH
KEMENTERIAN PELAJARAN MALAYSIA
PEPERIKSAAN PERTENGAHAN TAHUN TINGKATAN 5**

MATEMATIK TAMBAHAN

Kertas 1

Dua jam

**JANGAN BUKA KERTAS SOALANINI
SEHINGGA DIBERITAHU**

- 1 This question paper consists of **25** questions.
- 2 Answer all questions.
- 3 Give only one answer for each question.
- 4 Write your answers clearly in the spaces provided in the question paper.
- 5 Show your working. It may help you to get marks.
- 6 If you wish to change your answer, cross out the work that you have done. Then write down the new answer.
- 7 The diagrams in the questions provided are not drawn to scale unless stated.
- 8 The marks allocated for each question and sub-part of a question are shown in brackets.
- 9 A list of formulae is provided on pages 2 to 3.
- 10 A booklet of four-figure mathematical tables is provided.
- 11 You may use a non-programmable scientific calculator.
- 12 This question paper must be handed in at the end of the examination .

For examiner's use only

Question	Total Marks	Marks Obtained
1	2	
2	4	
3	2	
4	3	
5	3	
6	2	
7	3	
8	3	
9	3	
10	4	
11	4	
12	4	
13	4	
14	3	
15	3	
16	2	
17	4	
18	4	
19	4	
20	4	
21	3	
22	3	
23	3	
24	3	
25	3	
TOTAL	80	

Kertas soalan ini mengandungi 13 halaman bercetak

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SULIT

The following formulae may be helpful in answering the questions. The symbols given are the ones commonly used.

ALGEBRA

$$1 \quad x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$2 \quad a^m \times a^n = a^{m+n}$$

$$3 \quad a^m \div a^n = a^{m-n}$$

$$4 \quad (a^m)^n = a^{nm}$$

$$5 \quad \log_a mn = \log_a m + \log_a n$$

$$6 \quad \log_a \frac{m}{n} = \log_a m - \log_a n$$

$$7 \quad \log_a m^n = n \log_a m$$

$$8 \quad \log_a b = \frac{\log_c b}{\log_c a}$$

$$9 \quad T_n = a + (n-1)d$$

$$10 \quad S_n = \frac{n}{2}[2a + (n-1)d]$$

$$11 \quad T_n = ar^{n-1}$$

$$12 \quad S_n = \frac{a(r^n - 1)}{r-1} = \frac{a(1 - r^n)}{1-r}, \quad (r \neq 1)$$

$$13 \quad S_{\infty} = \frac{a}{1-r}, \quad |r| < 1$$

CALCULUS

$$1 \quad y = uv, \quad \frac{dy}{dx} = u \frac{dv}{dx} + v \frac{du}{dx}$$

$$2 \quad y = \frac{u}{v}, \quad \frac{dx}{dy} = \frac{v \frac{du}{dx} - u \frac{dv}{dx}}{v^2},$$

$$3 \quad \frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx}$$

$$4 \quad \text{Area under a curve}$$

$$= \int_a^b y \, dx \quad \text{or}$$

$$= \int_a^b x \, dy$$

$$5 \quad \text{Volume generated}$$

$$= \int_a^b \pi y^2 \, dx \quad \text{or}$$

$$= \int_a^b \pi x^2 \, dy$$

GEOMETRY

$$1 \quad \text{Distance} = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

$$2 \quad \text{Midpoint}$$

$$(x, y) = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

$$3 \quad |r| = \sqrt{x^2 + y^2}$$

$$4 \quad \hat{r} = \frac{xi + yj}{\sqrt{x^2 + y^2}}$$

$$5 \quad \text{A point dividing a segment of a line}$$

$$(x, y) = \left(\frac{nx_1 + mx_2}{m+n}, \frac{ny_1 + my_2}{m+n} \right)$$

$$6 \quad \text{Area of triangle}$$

$$= \frac{1}{2} \left| (x_1 y_2 + x_2 y_3 + x_3 y_1) - (x_2 y_1 + x_3 y_2 + x_1 y_3) \right|$$

STATISTICS

$$1 \quad \bar{x} = \frac{\sum x}{N}$$

$$2 \quad \bar{x} = \frac{\sum fx}{\sum f}$$

$$3 \quad \sigma = \sqrt{\frac{\sum (x - \bar{x})^2}{N}} = \sqrt{\frac{\sum x^2}{N} - \bar{x}^2}$$

$$4 \quad \sigma = \sqrt{\frac{\sum f(x - \bar{x})^2}{\sum f}} = \sqrt{\frac{\sum fx^2}{\sum f} - \bar{x}^2}$$

$$5 \quad m = L + \left[\frac{\frac{1}{2}N - F}{f_m} \right] C$$

$$6 \quad I = \frac{Q_1}{Q_0} \times 100$$

$$7 \quad \bar{I} = \frac{\sum w_i I_i}{\sum w_i}$$

$$8 \quad {}^n P_r = \frac{n!}{(n-r)!}$$

$$9 \quad {}^n C_r = \frac{n!}{(n-r)!r!}$$

$$10 \quad P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$11 \quad P(X = r) = {}^n C_r p^r q^{n-r}, \quad p + q = 1$$

$$12 \quad \text{Mean } \mu = np$$

$$13 \quad \sigma = \sqrt{npq}$$

$$14 \quad z = \frac{x - \mu}{\sigma}$$

TRIGONOMETRY

$$1 \quad \text{Arc length, } s = r\theta$$

$$2 \quad \text{Area of sector, } L = \frac{1}{2}r^2\theta$$

$$3 \quad \sin^2 A + \cos^2 A = 1$$

$$4 \quad \sec^2 A = 1 + \tan^2 A$$

$$5 \quad \operatorname{cosec}^2 A = 1 + \cot^2 A$$

$$6 \quad \sin 2A = 2 \sin A \cos A$$

$$7 \quad \begin{aligned} \cos 2A &= \cos^2 A - \sin^2 A \\ &= 2 \cos^2 A - 1 \\ &= 1 - 2 \sin^2 A \end{aligned}$$

$$8 \quad \tan 2A = \frac{2 \tan A}{1 - \tan^2 A}$$

$$9 \quad \sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$$

$$10 \quad \cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$$

$$11 \quad \tan(A \pm B) = \frac{\tan A \pm \tan B}{1 \mp \tan A \tan B}$$

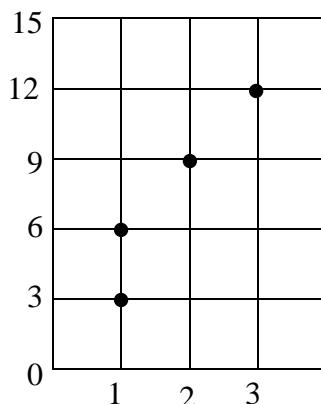
$$12 \quad \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$13 \quad a^2 = b^2 + c^2 - 2bc \cos A$$

$$14 \quad \text{Area of triangle} = \frac{1}{2}ab \sin C$$

Answer all questions.

1. Diagram 1 shows the relation between two sets of numbers .

**DIAGRAM 1**

State,

- (a) the image of 1,
(b) the type of relation

[2 marks]

1

2

*Answer : (a)**(b)*

-
2. Given $f : x \rightarrow \frac{5}{x}, x \neq 0$ and $g : x \rightarrow 3x + 6$. Find

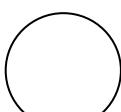
(a) $g^{-1}(x)$,

(b) $fg^{-1}(3)$.

[4 marks]

*Answer : (a)**(b)***2**

4



- 3 Form the quadratic equation which has the roots $-\frac{1}{3}$ and 4 .

Give your answer in the form $ax^2 + bx + c = 0$, where a , b and c are constants.

[2 marks]

Answer : (a)

3

2

- 4 A quadratic equation $2x^2 - x + p - 1 = 0$, has no roots.
Find the range of values of p .

[3 marks]

4

Answer :

3

- 5 Given that the roots of quadratic equation $2x^2 + (h-1)x + k = 0$ are -3 and 6.

Find

- (a) the value of h , [1 marks]
(b) the value of k . [2 marks]

Answer : (a)

5

(b)

3

- 6** It is given that the quadratic function $f(x) = 2[(x-3)^2 + 5]$.
(a) Write the equation of the axis of symmetry,
(b) State the coordinates of the minimum point.

[2 marks]

6

2

Answer : (a)

(b).....

-
- 7** Find the range of the values of x for $x(2x+5) \geq 12$.

[3 marks]

7

3

Answer :

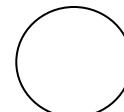
-
- 8** Solve the equation $\frac{4^{x-1}}{2} = 16^{x+1}$.

[3 marks]

8

3

Answer :



- 9** Solve the equation $\log_5(2x+3) = 1 + \log_5(x-1)$

[3 marks]

9

3

Answer :

- 10** Given that $\log_3 2 = m$ and $\log_3 5 = n$, express $\log_9 20$ in terms of m and n .

[4 marks]

10

4

Answer :

- 11** The 5th term of an arithmetic progression is 45 and the 7th term is 5.
Find

a) the first term and the common difference [2 marks]

b) the sum of the first six terms [2 marks]

Answer: a)

11

4

b)

12. The n th term of a geometric progression can be determined by using the formula $T_n = 2^{3 - 2n}$. Calculate

- a) the common ratio of the progression. [2 marks]
- b) the sum to infinity. [2 marks]

12

4

Answer : a)

b)

13. Diagram 3 shows a linear graph of xy against $\frac{1}{x}$.

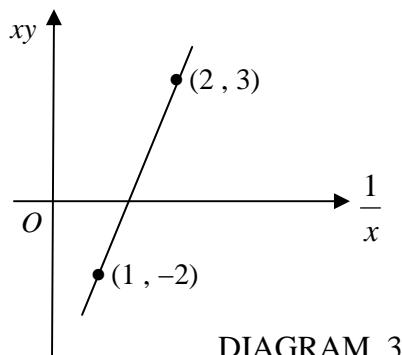


DIAGRAM 3

- (a) Express y in terms of x . [3 marks]
- (b) Find the value of y when $x = 4$ [1 marks]

13

4

Answer : (a)

(b)

- 14** The points $P(2k, k)$, $Q(h, t)$ and $R(2h, 3t)$ are on a straight line. Q divides PR internally in the ratio 2:3. Express h in terms of t

[3 marks]

14

3

Answer : $h = \dots\dots\dots$

- 15** Given point $R(-2, 0)$ and point $S(2, 3)$. Point P moves such that $PR : PS = 3 : 2$. Find the equation of the locus of P .

[3 marks]

15

3

Answer : $\dots\dots\dots$

- 16** Diagram 3 shows a triangle OAB such that $\vec{OA} = \underline{a}$, $\vec{OB} = \underline{b}$ and $2\vec{AP} = \vec{AB}$

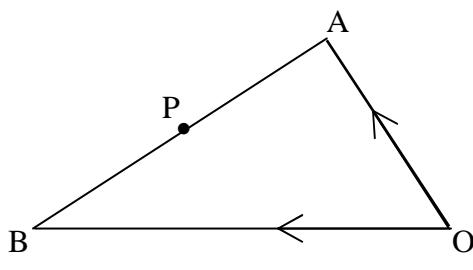


DIAGRAM 3

Find \vec{OP} in terms of \underline{a} and \underline{b}

[2 marks]

16

2

Answer : $\dots\dots\dots$ **[Lihat sebelah**
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17. Diagram 4 shows vectors \overrightarrow{OR} , \overrightarrow{OS} and \overrightarrow{OT} drawn on a Cartesian plane.

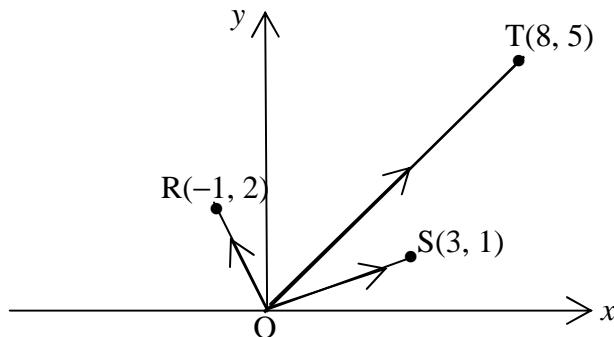


DIAGRAM 4

Find the value of m and n such that $\overrightarrow{OR} + m\overrightarrow{OS} = n\overrightarrow{OT}$.

[4 marks]

17

4

Answer :

18. Table 2 shows the number of story books read by a group of students in a certain school.

Number of story books read	0	1	2	3
Number of students	7	9	3	x

TABLE 2

- (a) State the largest possible value of x given that the mode is 1. [1 mark]
(b) State the largest possible value of x given that the median is 1. [1 mark]
(c) Calculate the value of x given that the mean is 1. [2marks]

18

4

Answer : a).....

b).....

c).....

- 19 Diagram 5 shows a circle with centre O. The length of the radius is 2.5 cm and the area of sector AOB is 6.25 cm^2 .

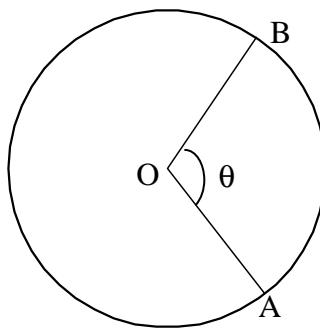


DIAGRAM 5

Calculate

- (a) the value of θ [2 marks]
(b) the perimeter of the sector AOB . [2 marks]

19*Answer : (a).....*

4

(b).....

-
- 20 Solve the equation $\cos 2x - \cos x = 0$ for $0^\circ \leq x \leq 360^\circ$.

[4 marks]

20*Answer :*

4

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- 21** It is given that $\sin A = p$, $0^\circ < A < 90^\circ$
Find
(a) $\cos (90^\circ - A)$
(b) $\sin 2A$
in terms of p

[3 marks]

21

3

Answer : (a)
(b)

-
- 22** The curve $y = x^2 - 3x + 2$ has a gradient of 2 at point $P (t, 5)$.
Find

- (a) the value of t .
(b) the equation of the normal at point P .

[3 marks]

22

3

Answer : (a).....
(b)

-
- 23.** Given that $y = 2x(x - 5)$. Find the rate of change of y at $(2, 1)$ when the rate of
change of x is 3 units per second

[3 marks]

23

3

Answer :

24 Given that $\int_k^0 (2x + 3)dx = -4$, where k is a constant. Find the possible value of k .

[3 marks]

24

Answer :

3

25. Given that $y = \frac{3x+1}{x^2}$ and $\frac{dy}{dx} = 4k(x)$ with $k(x)$ is a function in terms of x .

Find the value of $\int_{-1}^1 k(x) dx$.

[3 marks]

25

END OF THE QUESTION PAPER

3